Anisotropic wall permeability effects on turbulent channel flows

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Kazuhiko Suga[1]†, Yuki Okazaki[1], Unde Ho[1] and Yusuke Kuwata[1]

[1]Department of Mechanical Engineering, Osaka Prefecture University, Osaka 599-8531, Japan

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Streamwise-wall-normal (x–y) and streamwise-spanwise (x–z) plane measurements are carried out by planar particle image velocimetry for turbulent channel flows over anisotropic porous media at the bulk Reynolds number Re_b=900–13600. Three kinds of anisotropic porous media are constructed to form the bottom wall of the channel. Their wall permeability tensor is designed to have a larger wall-normal diagonal component (wall-normal permeability) than the other components. Those porous media are constructed to have three mutually orthogonal principal axes and those principal axes are aligned with the Cartesian coordinate axes of the flow geometry. Correspondingly, the permeability tensor of each porous medium is diagonal. With the x–y plane data, it is found that the turbulence level well accords with the order of the streamwise diagonal component of the permeability tensor (streamwise permeability). This confirms that the turbulence strength depends on the streamwise permeability rather than the wall-normal permeability when the permeability tensor is diagonal and the wall-normal permeability is larger than the streamwise permeability. To generally characterize those phenomena including isotropic porous wall cases, modified permeability Reynolds numbers are discussed. From a quadrant analysis, it is found that the contribution from sweeps and ejections to the Reynolds shear stress near the porous media are influenced by the streamwise permeability. In the x–z plane data, although low- and high-speed streaks are also observed near the anisotropic porous walls, large-scale spanwise patterns appear at a larger Reynolds number. It is confirmed that they are due to the transverse waves induced by the Kelvin-Helmholtz instability. By the two-point correlation analyses of the fluctuating velocities, the spacing of the streaks and the wavelengths of the Kelvin-Helmholtz waves are discussed. It is then confirmed that the transition point from the quasi-streak structure to the roll-cell like structure is characterized by the wall-normal distance including the zero plane displacement of the log-law velocity which can be characterized by the streamwise permeability. It is also confirmed that the normalized wavelengths of the K-H waves over porous media are in the similar range to that of the turbulent mixing layers irrespective of the anisotropy of the porous media.

Key words:

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1. Introduction

The surfaces of real materials are usually not hydraulically smooth but have roughness. In many such cases, flows are turbulent and sometimes the fluids permeate through the wall materials. Accordingly, many studies tried to reveal turbulent flow characteristics

† Email address for correspondence: suga@me.osakafu-u.ac.jp

over permeable porous surfaces (e.g. Lovera & Kennedy 1969; Ruff & Gelhar 1972; Ho & Gelhar 1973; Zagni & Smith 1976; Zippe & Graf 1983; Kong & Schetz 1982; Shimizu *et al.* 1990; Pokrajac & Manes 2009; Manes *et al.* 2009; Detert *et al.* 2010; Suga *et al.* 2010, 2011, 2013; Manes *et al.* 2011). The permeability was defined in the convection theory through porous media by Darcy (1856) who found proportionality between flow rates and pressure differences applied to uniform porous media. Whitaker (1986) theoretically derived this Darcy's law as

$$\langle u_i \rangle = -\frac{K_{ij}}{\mu}\left(\frac{\partial \langle p \rangle^f}{\partial x_j} - \rho g_j\right), \tag{1.1}$$

where K_{ij}, $\langle u_i \rangle$, $\langle p \rangle^f$, g_j, μ and ρ are the permeability tensor, the superficially volume averaged velocity u_i, the volume averaged fluid-phase pressure, the gravitational acceleration, the dynamic viscosity and the density of the fluid, respectively. Although the permeability is a second order symmetric tensor (Whitaker 1969, 1996; Guin *et al.* 1971; Szabo 1968; Case & Cochran 1972), most studies on flows over porous media applied isotropic porous media and thus did not consider anisotropic permeability effects. Even though Kong & Schetz (1982) measured flows over anisotropic porous media such as perforated titanium sheets and bonded screen sheets, they did not discuss the anisotropic effects. Of course, in cases that the structures of the porous media are isotropic, it does not cause any problem to define one of the diagonal components of the permeability tensor as the "permeability" of the material. In fact, it has been usually applied in the literature as in Zagni & Smith (1976); Zippe & Graf (1983); Pokrajac & Manes (2009); Suga *et al.* (2010); Manes *et al.* (2011).

From those studies, what was confirmed was that the wall permeability affects the turbulent flow structure near wall surfaces enhancing momentum exchange. Since a permeable wall allows turbulent eddy vortex motions to penetrate into the wall, turbulence is not totally damped unlike near a solid wall resulting in strong wall shear. This has been also proven by the direct numerical simulation (DNS) studies (Breugem *et al.* 2006; Chandesris *et al.* 2013; Rosti *et al.* 2015; Kuwata & Suga 2016*a*) of turbulent porous walled channel flows. The DNSs by Breugem *et al.* (2006); Kuwata & Suga (2016*a*) and the particle image velocimetry (PIV) experiments by Suga *et al.* (2010, 2011, 2017); Suga (2016) for turbulent channel flows over isotropic porous media indicated correlations between the inner phenomena and the permeability Reynolds number defined as $Re_K = u_\tau^p \sqrt{K}/\nu$ based on the friction velocity u_τ^p on the porous wall, the wall permeability K and the fluid kinematic viscosity ν. Suga *et al.* (2010, 2017) suggested that the von Kármán coefficient κ, the zero plane displacement d and the roughness scale h of the mean velocity profiles were well correlated to the permeability Reynolds number. Manes *et al.* (2011) performed laser Doppler anemometer (LDA) measurements for turbulent boundary layers over polyurethane foam and suggested that the shear penetration depth and the boundary layer thickness could be used respectively for the inner and outer length scales of boundary layers.

As for the near-wall turbulence structure, the DNS and PIV studies(Breugem *et al.* 2006; Suga *et al.* 2011, 2017; Kuwata & Suga 2016*a*,*b*) reported that the streaky structure was destroyed in the turbulent porous walled channel flows by the wall permeability effects. Above a highly permeable wall, Breugem *et al.* (2006) concluded that turbulent transport across the permeable wall prevented the development of elongated streaks. From the comparison between the results of permeable and impermeable rough wall cases, Kuwata & Suga (2016*a*) concluded that over the permeable wall, the vortex structure became shredded and the streamwise coherent structure became shorter due to

the wall roughness whereas the streaks over the permeable wall tended to be vaguer and its spanwise pitch became approximately twice as wide as that over the impermeable walls. By analysing the PIV data in streamwise-wall-normal (x-y) planes, Suga *et al.* (2011) showed that the structure tended to be disordered with the increase of the wall permeability while it looked similar to that in an impermeable wall boundary layer at a lower wall permeability. The quadrant analysis confirmed that sweeps became most dominant very near the permeable wall whilst that of ejections overtook them in the buffer region. As the wall permeability increased, stronger sweeps tended to move toward the wall though ejections tended to lose their strength since the fluid pushed out from the porous wall by the strong inward penetrating motions had already lost its energy inside the porous wall. Accordingly, these phenomena led to shortened longitudinal vortices since vortex motions could not be maintained with the weakened ejections over highly permeable walls. From the PIV data in streamwise-spanwise (x–z) planes, Suga *et al.* (2017) found that the spanwise spacing of the streaks and the spanwise integral length could be reasonably correlated with the wall normal distance including the zero-plane displacement of the log-law mean velocity profile. Since the zero-plane displacement d is considered to be a length scale associated with the penetration, the distribution profiles of those scales indicated that the structure maintained the characteristics of streaks even if their bottom parts penetrated into the porous walls by the downward motions of the Kelvin-Helmholtz (K-H) waves. Accordingly, the surviving elements of the streaks existed and their scales maintained correlations with the wall normal distance under the transitional range starting from $(y + d)^{p+} \simeq 100$, while those elements tended to be disturbed by the K-H instability as the wall normal distance increases. Here, $(\cdot)^{p+}$ is a normalized value using the friction velocity at the porous wall. Above the transitional region, flow motions with much larger spanwise length scales started to be dominant. Such flow motions were considered to be transverse roll cells which were generated by the K-H instability and destroyed the longitudinal vortex trails.

Although the above mentioned understandings are pieces to construct the fluid dynamics over porous media, we need further knowledge of the anisotropic permeability effects to make it complete. Correspondingly, for turbulent flows over anisotropic porous media, Kuwata & Suga (2017) recently performed a direct numerical simulation. They applied four kinds of porous media whose structures were designed ideally to have anisotropic components of the permeability tensor. The considered porous media were walls with square pore arrays aligned with the Cartesian axes, namely walls with only the wall-normal diagonal component, with the wall-normal and streamwise diagonal components, with the vertical and spanwise diagonal components, and with the isotopic wall-normal, spanwise and streamwise diagonal components of the permeability tensor. It was found that turbulence was not altered by the wall-normal diagonal component of the permeability tensor (called the wall-normal permeability, hereafter for simplicity) itself whilst the streamwise and spanwise components (streamwise and spanwise permeabilities, hereafter) considerably enhanced turbulence over the porous walls. It was revealed that enhancement of turbulence was more remarkable over porous media with streamwise permeability.

Except for the above knowledge, we do not know the anisotropic permeability effects on turbulence over porous media at all. Therefore, in this study planar PIV measurements of turbulence over anisotropic porous media are carried out. Using polymer nets, three kinds of anisotropic porous layers are constructed to form a bottom wall of fully developed turbulent channel flows. Their wall normal component of the permeability tensor is designed to be larger than the other components by the factor of 1.2, 1.5 and 173. Those porous media are constructed to have three mutually orthogonal principal axes.

Hence, their permeability tensors are diagonal and they are called orthotropic porous media(Dullien 1979). Measurements of the streamwise-wall-normal (x–y) planes are carried out to reveal the turbulence characteristics. The range of the measured Reynolds number is Re_b=900–13600 to cover laminar to turbulent flows. To understand the spanwise turbulence structure measurements of the streamwise-spanwise (x–z) planes are also carried out.

2. Experimental method

To construct the porous media, ethylene vinyl acetate (EVA) copolymer nets (N-523, Takiron) with rounded-square shaped pores shown in figure 1(a) are applied. Although one side of the net has a ribbed structure, the reverse side has a smooth surface. The porous media have layered structures of the unit layers which are formed by bonding two nets as shown in figure 1(b). Figure 2 shows three kinds of porous media made by different piling patterns of the layers in which the pore arrays are aligned with the Cartesian axes of the flow geometry. Since the specific gravity of the EVA is 0.92–0.95, to increase the weight of the porous media lead plates are bonded to the very bottom layers. Porous medium case O is constructed by piling up the unit layers straightly while case Θ is made by offset staggered piling-up. Case Φ is the same porous medium as case Θ but its setting angle to the flow direction is turned 90 degree. Note that cases O, Θ and Φ are named from the top views of the meshes. As seen in figure 2, all the structures have three mutually orthogonal principal axes and those principal axes are aligned with the Cartesian coordinate axes. In such cases, the porous media are called the orthotropic porous media and their permeability tensors become diagonal (Dullien 1979). (This can be easily proven by manipulating Darcy's law with macroscopic symmetry conditions.)

The characteristics of the porous media are measured by the method as follows. For the porosity φ that is the ratio of the fluid phase volume V_f and the total volume V_m: $\varphi = V_f/V_m$, by measuring perimeters of sample rectangular parallelepiped blocks, V_m is obtained and its solid phase volume V_s is obtained by sinking the sample blocks into water contained in a measuring cylinder. Diagonal components of the permeability tensor $K_{\alpha\alpha}$ and the Forchheimer tensor $F_{\alpha\alpha}$ are measured using a duct flow facility. In between the pressure holes, a porous block is placed to block the duct. Pressure drops $\partial \langle p \rangle^f / \partial x_\alpha$ along the α–axis of the media and flow rates are measured by a differential pressure gauge and a flow meter, respectively. With those variables at several different flow rates, the diagonal components of the permeability and Forchheimer tensors are obtained using the Darcy-Forchheimer equation of Whitaker (1986):

$$\langle u_i \rangle = -\frac{K_{ij}}{\mu} \frac{\partial \langle p \rangle^f}{\partial x_j} - F_{ij} \langle u_j \rangle , \tag{2.1}$$

where F_{ij} is the Forchheimer tensor and currently modelled as $F_{ij} = \rho C^F_{ij} |\langle \mathbf{u} \rangle| / \mu$ following the model by Nakayama *et al.* (2002) while their Forchheimer coefficient tensor B^F_{ij} was defined by $F_{ij} = \rho K_{ik} B^F_{kj} |\langle \mathbf{u} \rangle| / \mu$. (In their case, the Forchheimer tensor explicitly depends on the permeability tensor.) The Darcy velocity $\langle u_i \rangle$ is obtained from the measured flow rate. Note that for the material whose structure is symmetric in the x-, y- and z-directions, the Forchheimer tensor becomes diagonal. (This can be proven by manipulating equation (2.1) with the symmetry conditions.) As seen in figure 2, the structures of the present porous media are symmetric in the x- and z-directions while they are not strictly symmetric in the y-direction. The side-views of the pore-shapes are asymmetric in the y-direction though they are not very far from symmetric. Hence, we

assume that the effects of the off-diagonal components of the Forchheimer tensor on the measurement of the characteristics of the porous media are insignificant. The measured valuables of the present porous media are listed in table 1. Although the porosity is constant for all three cases as φ=0.7, to study the effects of the anisotropic permeability on turbulence, the wall-normal diagonal component of the permeability tensor K_{yy} is designed to be larger than the other components by the factor of 1.2, 1.5 and 173. As for the Forchheimer tensor, the coefficient C_{ij}^F is nearly isotropic in cases Θ and Φ while it is anisotropic in case O with larger C_{yy}^F than the other components by the factor of 76.

Figure 3(a) illustrates the experimental flow facility. Tap water whose temperature is maintained by a cooler at 285±1 K is pumped to a digital flow meter (FD-MH200A/500A, KEYENCE) where its total flow rate is measured. The water temperature is recorded by a digital thermometer (FD-T1, KEYENCE) in a honeycomb-bundled nozzle. After the flow is conditioned by the honeycomb-bundled nozzle and fully developed in a driver section whose length is 3.0 m, it enters the test section whose length is 1.0 m. As illustrated in figure 3(b), both the sections consist of solid smooth acrylic walls with a porous bottom layer. The sectional width W and the total height are, respectively, 0.3 m and 0.06 m which is filled by a 0.03 m thick porous layer. Since the height of the clear fluid region is set to H=0.03 m, the aspect ratio of the cross section of the clear fluid region is about 10. Accordingly, two-dimensionality can be reasonably attained in z/W =0.1−0.9 which was confirmed and reported by the previous study (Suga *et al.* 2017). The measured range of the bulk Reynolds number Re_b ($\rho U_b H/\mu$) is 900–13600 where the fluid viscosity μ and density ρ are determined by the measured water temperature. Here, the bulk mean velocity U_b is obtained by integrating the measured cross-sectional streamwise mean velocity distribution while the wall shear stress is estimated by extrapolating the Reynolds shear stress distribution obtained by the x–y plane measurement.

The applied planar PIV system consists of a double-pulse Nd-YAG laser (Dual Power 200-15, Litron) with 200 mJ per pulse at a wavelength of 532 nm. For the measurements of the streamwise-wall-normal (x–y) planes, the laser beam is formed into a sheet of approximately 1.0 mm thickness through several cylindrical lenses and illuminates the measuring planes as shown in figure 3(c). The recorded frame of a CCD camera (Flowsense 4M Mk2, DANTEC DYNAMICS) operating at 30 f.p.s with 85 mm $f/1:8$ lenses (AF Nikkor, Nikon) covers a section of 30(x)× 30(y) mm^2 locating in the middle part of the test section with 2048×2048 pixels. This frame covers four pore-cells of the porous media in the x-direction. To obtain the x–z plane averaged time mean quantities in the y-direction, the flow fields are measured at four x–y sections: A, B, C and D from the symmetry plane of the channel as shown in figure 3(d). Using time mean field data, streamwise averaging is carried out for each section. Then, with the streamwise averaged data of the four sections, integration by the trapezoidal rule is applied to the spanwise averaging. It has been confirmed that the four plane measurements are good enough for the spanwise averaging by comparing the results with those obtained by the measurement of six planes which divide the unit pore-cell equally (1.25 mm pitch). Note that the integration by the six plane measurement data is nearly ideal for the volume averaging since the pore pitch and the approximate laser sheet thickness are 7.5 mm and 1 mm, respectively. Accordingly, the present plane averaged values are from the plane of 4(x) × 1(z) pore-cells of the porous media. For the measurements of the streamwise-spanwise (x–z) planes, the laser sheet of approximately 1.0 mm thickness illuminates the x–z planes as shown in figure 3(e). Two CCD cameras are arranged in tandem. The recorded frame of each CCD camera covers a zone of 81×81 mm^2 located in the middle of the test section with 2048×2048 pixels, for which 10% of the area overlaps with another

camera's frame. The measured planes are located at y =1.0, 2.0, 3.0, 4.0, 5.0 mm while additional planes are occasionally measured. Note that the origin of the y–axis is set at the porous surface.

For the tracer particles of the x–y plane measurements, acrylic colloid particles are used. The mean diameter, specific gravity and refractive index of the particles are respectively 3.1 μm, 1.19 and 1.50. For the x–z plane measurements, to avoid the noisy Mie scattering from the wall surface, polymer fluorescent particles containing Rhodamine B, whose mean diameter and specific gravity are respectively 10 μm and 1.50, are used. Correspondingly, a long-pass filter with cutoff wavelength 560 nm is located in front of each camera lens. In both cases, the seeding density is adjusted to obtain 10-15 particle-image pairs in each interrogation window whose size is set to 32×32 pixels. Thus the measurement sampling volumes are $0.4(x) \times 0.4(y) \times 1.0(z)$ mm^3 and $0.4(x) \times 1.0(y) \times 0.4(z)$ mm^3, respectively for the x–y and x–z measurements. The image sampling rate was 4 Hz. The average particle displacement was set to be about 25 % length (6-8 pixels) of the interrogation window. To obtain the statistical data more than 4000 image pairs are processed. The recorded data are processed by Dynamics Studio 3.1 software (DANTEC DYNAMICS) with the fast Fourier transform cross-correlation technique (Willert & Gharib 1991). Each image is processed to produce 127× 127 vectors from the interrogation windows with 50 % overlap in each direction. When the ratio of the first and the second correlation peaks in an interrogation window is smaller than 1.3, it is removed from the process as an error vector. Furthermore, the moving-average validation (Host-Madsen & McCluskey 1994) is applied with an acceptance factor of 0.1. In the present study, the removed error vectors are less than 3 % of the total data processed.

Following Prasad *et al.* (1992), it is confirmed that the particle images are well resolved in the present experiments, and the uncertainty in the measured displacement can be expected to be approximately less than 1/10 of the diameter of the particle image. Normalizing this uncertainty by the mean displacement length of particles indicates that the estimated error of the magnitude of the instantaneous velocity is less than 4% of the maximum velocity near the channel centreline.

3. Results and discussions

3.1. *Streamwise-wall-normal plane measurements*

Table 2 lists the experimental conditions and measured parameters which are discussed below. For case O, the measured flows are at Re_b=900, 1300, 3600, 4800, 10500 and 13600 while for cases Θ and Φ they are at Re_b= 3400, 5000, 10300, 13600 and Re_b= 3400, 5700, 10400, 13600, respectively. In the following discussions, the x–z plane averaged value of ϕ is denoted as $[\phi]$ and the Reynolds averaged ϕ is denoted as $\bar{\phi}$ with the Reynolds decomposition: $\phi = \bar{\phi} + \phi'$. For simplicity, the plane and Reynolds averaged velocity is called the "mean velocity" hereafter.

3.1.1. *Mean velocity*

Figure 4 shows the streamwise mean velocity $[U]$ $(=[\bar{u}_x])$ profiles. In case O, as seen in figure 4(a) at Re_b = 900 the velocity profile is parabolic implying that the flow is laminar but from Re_b = 1300 the profile becomes asymmetrical indicating that the laminar to turbulent transition occurs in this range of the Reynolds number. Once the flow becomes fully turbulent at $Re_b \geqslant 3600$, there is no significant change in the profiles. This tendency and the general slanted profiles to the porous walls are maintained in cases Θ and Φ as seen in figure 4(b) and (c). The slippage velocities on the porous surfaces are

approximately $[U_w]/U_b = 0.4$ at $Re_b \geqslant 3600$ which are similar to those over isotropic porous media reported in the previous study (Suga *et al.* 2010). These velocity profiles are replotted in semi-logarithmic charts as shown in figure 5. The fitted lines are of the log-law form that is usually applied to the flows over porous media and canopies (Best 1935; Nikora *et al.* 2002; Nepf & Ghisalberti 2008). That is

$$[U]^{p+} = \frac{1}{\kappa} \ln\left(\frac{y+d}{h}\right), \tag{3.1}$$

with the von Kármán constant κ, the zero-plane displacement d and the roughness scale h. Here, $[U]^{p+} = [U]/u_\tau^p$ and the friction velocity u_τ^p on the porous wall is estimated by extrapolating the plane averaged Reynolds shear stress distribution measured by this study. Figure 6(a) shows illustrative definition of d and h. They are the displacement of the origin of the y-axis and the equivalent roughness-height from the zero-plane, respectively. Table 2 lists the values of κ, $d^{p+}(= u_\tau^p d/\nu)$ and $h^{p+}(= u_\tau^p h/\nu)$ which are obtained as follows. The extent of the logarithmic layer can be determined from plots of $(y+d)\mathrm{d}[U]^{p+}/\mathrm{d}y$ as a function of $y^{p+}(= yu_\tau^p/\nu)$ changing the values of d (Breugem *et al.* 2006). Since $(y+d)\mathrm{d}[U]^{p+}/\mathrm{d}y$ must be a constant equal to $1/\kappa$ inside the logarithmic layer, a value of d giving a flat plateau in the profile must be the best fitted value. For example, in figure 6(b), a flat plateau can be obtained with $d^{p+} = 51.5$ and the value of the plateau becomes $(y+d)\mathrm{d}[U]^{p+}/\mathrm{d}y$=3.5 which corresponds to $1/\kappa$ to be obtained. Then, with these d and κ, equation (3.1) is best fitted to the velocity profile to obtain the roughness length scale h.

It is obvious that the slope of the fitted line, and hence κ varies with Re_b. This trend is the same as that reported in the previous studies (Suga *et al.* 2010, 2017) in which obvious correlations between the permeability Reynolds number Re_K and the parameters: κ , d and h were reported. However, as shown in figure 7 it is seen that such correlations with Re_K cannot be seen in the present data, particularly for d and h. For the anisotropic porous media, K is currently defined as

$$K = K_{kk}/3 = (K_{xx} + K_{yy} + K_{zz})/3, \tag{3.2}$$

which corresponds to 1/3 of the trace of the permeability tensor and maintains consistency with the isotropic permeability. Hence, in this study the permeability Reynolds number is defined as

$$Re_K = \frac{u_\tau^p \sqrt{K_{kk}/3}}{\nu}. \tag{3.3}$$

Table 2 lists Re_K for each case. Since the values of Re_K in case O are significantly larger than those in cases Θ and Φ, the plots of case O in figure 7 significantly deviate from the other plots. Also, another form: $K = (K_{xx}K_{yy}K_{zz})^{1/3}$, whose concept is from Chan *et al.* (1993), leads to much larger values of Re_K in case O and produces more unsuccessful results than those shown in figure 7. These results suggest that anisotropic effects of the permeability and/or the Forchheimer tensor play important roles in determining the flow characteristics.

3.1.2. *Generalization of the characteristic Reynolds number*

Since the zero-plane displacement d and the roughness scale h are defined as the values inside porous surfaces, we discuss on the transport equations inside porous media. In the double (Reynolds and volume) averaging process, Pedras & de Lemos (2000) proved that the order of the averaging operations is interchangeable. When the following decomposition for the volume averaging: $\phi = \langle\phi\rangle + \tilde{\phi}$, is applied, the interchangeable

operations lead to $\overline{\langle\phi\rangle} = \langle\bar{\phi}\rangle$, $\langle\phi\rangle' = \langle\phi'\rangle$, $\tilde{\phi}' = (\tilde{\phi})'$ and $\bar{\tilde{\phi}} = \bar{\tilde{\phi}}$. Then, the double-averaged continuity and momentum equations in porous media may be written as

$$\frac{\partial\varphi\langle\bar{u}_i\rangle^f}{\partial x_i} = 0, \tag{3.4}$$

$$\frac{\partial\langle\bar{u}_i\rangle^f}{\partial t} + \langle\bar{u}_j\rangle^f\frac{\partial\langle\bar{u}_i\rangle^f}{\partial x_j} = -\frac{1}{\rho}\frac{\partial\langle\bar{p}\rangle^f}{\partial x_i} + \nu\frac{\partial^2\langle\bar{u}_i\rangle^f}{\partial x_j^2} - \frac{1}{\varphi}\frac{\partial}{\partial x_j}(\varphi\langle R_{ij}\rangle^f) - \frac{1}{\varphi}\frac{\partial}{\partial x_j}(\varphi\langle T_{ij}\rangle^f) - \bar{f}_i, \tag{3.5}$$

where the symbolic notations of the volume averaged Reynolds stress and the dispersion stress (or dispersive covariance; Raupach & Shaw (1982)) are $\langle R_{ij}\rangle^f = \langle\overline{u_i'u_j'}\rangle^f$ and $\langle T_{ij}\rangle^f = \langle\bar{\tilde{u}}_i\bar{\tilde{u}}_j\rangle^f$, respectively. Note that for the volume averaging, there is a relation: $\varphi\langle\phi\rangle^f = \langle\phi\rangle$. With the link to equation (2.1), the drag force term f_i derived by Whitaker (1996) is

$$f_i = \underbrace{\varphi\mu K_{ij}^{-1}\langle u_j\rangle^f}_{\text{viscous drag}} + \underbrace{\varphi\mu K_{ik}^{-1}F_{kj}\langle u_j\rangle^f}_{\text{form drag}}. \tag{3.6}$$

Accordingly, when K_{ij} is diagonal and the Forchheimer tensor is modelled as $F_{ij} = \rho C_{ij}^F|\langle\mathbf{u}\rangle|/\mu$, the force terms for the double averaged fields of fully developed flows (the streamwise and normal directions are aligned with the x- and y-axes, respectively) are

$$\bar{f}_x = \mu K_{xx}^{-1}\langle\bar{u}_x\rangle + \rho K_{xx}^{-1}\left\{C_{xx}^F\left(\overline{|\langle\mathbf{u}\rangle|\langle\bar{u}_x\rangle} + \overline{|\langle\mathbf{u}\rangle|'\langle u'_x\rangle}\right) + C_{xy}^F\left(\overline{|\langle\mathbf{u}\rangle|'\langle u'_y\rangle}\right)\right\}, \tag{3.7}$$

$$\bar{f}_y = \rho K_{yy}^{-1}\left\{C_{yx}^F\left(\overline{|\langle\mathbf{u}\rangle|'\langle u'_x\rangle}\right) + C_{yy}^F\left(\overline{|\langle\mathbf{u}\rangle|'\langle u'_y\rangle}\right)\right\}, \tag{3.8}$$

since $\langle\bar{u}_y\rangle = \langle\bar{u}_z\rangle = 0$. The above equation (3.7) indicates that the streamwise permeability K_{xx} directly affects the streamwise mean velocity inside porous media with the x-x and x-y components of C_{ij}^F. Furthermore, as shown in equation (3.5), since the double averaged momentum equation includes the contribution from the volume averaged Reynolds stress $\langle R_{ij}\rangle^f$ and the dispersion stress $\langle T_{ij}\rangle^f$, the budget terms of the shear stresses $\langle R_{xy}\rangle^f$ and $\langle T_{xy}\rangle^f$ should be considered for the streamwise velocity. (See Appendix A for the stress transport equations.) Among them there is no drag force related term in the $\langle R_{ij}\rangle^f$ transport equation (A 1) as derived by Pinson *et al.* (2006); Nezu & Sanjou (2008); Kuwata & Suga (2015), but the drag work term $\bar{f}_i\langle\bar{u}_j\rangle + \bar{f}_j\langle\bar{u}_i\rangle$ appears in the $\langle T_{ij}\rangle^f$ transport equation (A 2) as shown in Pinson *et al.* (2006); Kuwata *et al.* (2014). Hence, $\bar{f}_y\langle\bar{u}_x\rangle$ affects the mean velocity profile indirectly via $\langle T_{xy}\rangle^f$. Accordingly, coupling with the Forchheimer terms, K_{yy} influences the streamwise velocity as the Reynolds number increases. However, it is expected that the primary effect on the mean flow profile comes from the streamwise permeability K_{xx} via $\bar{f}_x$ when the Reynolds number is not significantly high. (Note that this is for the diagonal K_{ij} cases and not for the general anisotropic cases.) Furthermore, considering the fact that meaningful classification of turbulent flows by the permeability Reynolds number was reported by Breugem *et al.* (2006) at $Re_b = 5500$ and by Manes *et al.* (2011) at $Re_b < 10^5$, the following discussion focuses on modifying the permeability Reynolds number using the streamwise permeability.

Although simply replacing K with K_{xx} for Re_K may improve the correlation, to include the effects of the porosity in the characterization, we consider the Kozeny-Carman

equation (Kozeny 1927; Carman 1937, 1956):

$$\frac{d\left\langle p\right\rangle ^{f}}{dx}=-\frac{150\mu}{d_{g}^{2}\Phi_{s}^{2}}\frac{(1-\varphi)^{2}}{\varphi^{3}}\left\langle u_{x}\right\rangle ,\tag{3.9}$$

where Φ_s is the sphericity of the particles in the packed bed and d_g is the diameter of the related spherical particle. Combining equation (3.9) with the Darcy equation (1.1) yields the following relationship between d_g and permeability as $\sqrt{\frac{180(1-\varphi)^2}{\varphi^3}K_{xx}}=d_g$, where $150/\Phi_s^2$ is replaced by 180 following Macdonald *et al.* (1979). When K_{xx} is measurable, the newly defined length scale $d_{K_x}=\sqrt{\frac{180(1-\varphi)^2}{\varphi^3}K_{xx}}$ may be regarded as a characteristic streamwise length scale for the porous medium rather than the particle diameter. Using d_{K_x}, a characteristic Reynolds number:

$$Re_{K}^{*}=\frac{u_{\tau}^{p}d_{K_{x}}}{\nu}=\frac{u_{\tau}^{p}\sqrt{K_{xx}}}{\nu}\sqrt{\frac{180(1-\varphi)^{2}}{\varphi^{3}}},\tag{3.10}$$

which is a function of the porosity and the streamwise permeability, is called the "generalized" permeability Reynolds number in this study. The point that should be emphasized is that the length scale of Re_K^* is neither the pore nor grain diameter of a porous medium but a characteristic streamwise length scale defined by the porosity and the streamwise permeability. Figure 8 confirms that this generalized permeability Reynolds number Re_K^* is successful to characterize the turbulence over the present anisotropic porous media as well as the isotropic cases of Suga *et al.* (2010, 2017) though the plotted data of the von Kármán constant κ are somewhat more scattered. By performing the linear stability analysis, Tilton & Cortelezzi (2008) suggested that inertial effects can be considered negligible if the ratio between the square root of permeability and the channel half-width does not exceed 0.02. Indeed, in the present porous media $\sqrt{K_{xx}}/(H/2)$ does not exceed 0.02.

When the streamwise permeability does not exist, it is obvious that one encounters difficulty with Re_K^*. Moreover, it is not very convenient for engineers to directly measure permeabilities of the materials they want to apply to products. In fact, to obtain the permeability, Detert *et al.* (2010) applied the experimental correlation of Hazen (1892) for their laboratory measurements. Accordingly, a further discussion for an alternative candidate of the characteristic Reynolds number is carried out. Since the length scale in equation (3.10) is a streamwise characteristic length scale, it may be considered that there is a correlation between d_{K_x} and pore dimensions. After non-exhaustive search among possible candidates, our empirical attempt has selected the streamwise length D_{p_x} of the surface pore to surrogate d_{K_x}. Hence, the "surrogate" permeability Reynolds number may be

$$Re_{K}^{**}=c\frac{u_{\tau}^{p}D_{p_{x}}}{\nu},\tag{3.11}$$

where c is a constant to adjust the length scale. Interestingly, when $c=1/3.8$ is applied, an almost linear correlation between Re_K^* and Re_K^{**} can be seen as shown in figure 9. Note that when the surface pore is circular, D_{p_x} is its diameter while for a non-circular pore case D_{p_x} is simply defined as its streamwise length. Hence, for cases #20,#13 and #06, D_{p_x} corresponds to their pore diameters:1.7, 2.8, 3.8 mm, respectively, while for cases O, Θ, and Φ, D_{p_x}=5 mm. Consequently, this surrogate permeability Reynolds number, which is essentially a kind of modified pore Reynolds number, may be used to characterize general porous medium cases. Table 2 also lists Re_K^* and Re_K^{**} for the present cases.

To confirm the applicability of this surrogate permeability Reynolds number Re_K^{**} to

characterize porous-wall turbulence, figure 10 indicates all the data including the isotropic porous medium cases of #20, #13 and #06 as well as the experimental data of Detert *et al.* (2010); Manes *et al.* (2011) and numerical simulations of Breugem *et al.* (2006); Kuwata & Suga (2016*a*, 2017). For the cases of Detert *et al.* (2010) and Breugem *et al.* (2006), porous media consisting of sphere grains were considered. Hence, the hydraulic diameter using the specific surface a_v is applied as $D_{p_x} = 4\frac{\varphi}{a_v(1-\varphi)}$. When the grain shape is spheric with the diameter D_g, the specific surface becomes $a_v = 6/D_g$. The plots in figure 10 show reasonable correlations between the parameters and Re_K^{**} for all the porous wall cases. Indeed, the data correlate well for the zero-plane displacement d and the roughness scale h though the plotted data of the von Kármán constant κ are again somewhat more scattered. Note that even though a couple of cases of Kuwata & Suga (2017) do not have the streamwise permeability, Re_K^{**} can be applied to those cases. It is thus suggested that the proposed surrogate permeability Reynolds number: equation (3.11), is promising for the general correlation parameter of turbulence over porous media.

3.1.3. *Turbulence quantities*

Figure 11 compares the plane-averaged Reynolds shear stress $[-\overline{u'v'}]$ distribution profiles normalized by the bulk mean velocity U_b to see the difference depending on the bulk Reynolds number. As confirmed in figure 11(*a*), in case O, the flow is laminar at $Re_b = 900$ since $[-\overline{u'v'}]$ is almost zero across the channel. Then, at $Re_b = 1300$ the level of $[-\overline{u'v'}]$ increases indicating that the laminar to turbulent transition is taking place, and the other profiles suggest that the transition completes by $Re_b = 3600$. When the flow becomes turbulent, it is observed that the level of $[-\overline{u'v'}]$ near the porous wall ($y/H = 0.0$) becomes significantly higher than that near the solid top wall ($y/H = 1.0$). As seen in figure 11(*b, c*) for cases Θ and Φ, the trends at $Re_b \geqslant 3400$ look the same as that in case O. This confirms that the turbulence becomes significantly strong near the present porous media. Corresponding to the trend of the plane-averaged Reynolds shear stress, turbulent intensities: $[u']$ and $[v']$, which are the r.m.s. values of the plane-averaged Reynolds normal stresses, generally become higher in the bottom half of the channel than in the top half of the channel as seen in figure 12. Particularly, $[v']$ near the porous wall is considerably higher than near the top wall. Due to the relaxed wall-blocking effect by the porous surfaces, $[\overline{v'^2}]$ has larger values near the porous media than near the solid wall leading to the enhancement of the production of the plane-averaged Reynolds shear stress: $-[\overline{v'^2}]\partial[U]/\partial y$. Accordingly, turbulence level near the porous walls becomes high. This is the main reason why turbulence level becomes high near the porous media in many studies (e.g. Lovera & Kennedy 1969; Ruff & Gelhar 1972; Ho & Gelhar 1973; Zagni & Smith 1976; Zippe & Graf 1983; Kong & Schetz 1982; Breugem *et al.* 2006; Suga *et al.* 2010). However, when the slip velocity on the porous wall becomes much higher than the present ones due to higher porosity and/or permeability, the velocity gradient $\partial[U]/\partial y$ is expected to be considerably relaxed and this damps turbulence generation. In fact, in the rigid-vegetation-canopy flows of Nezu & Sanjou (2008), the friction velocity at $\varphi = 0.99$ reduced to be 84% of that at $\varphi = 0.97$ while it could not be confirmed which parameter controlled this tend since the permeabilities were unknown. In any case, although the relation between the surface turbulence and the porous parameters is considered to be non-monotonic, the present cases are in the range of turbulence enhancement.

Since the porosity is constant at $\varphi = 0.7$ in the present cases, it is possible to see the effects of the permeability. Figure 13 compares the plane-averaged Reynolds shear stress and turbulent intensity profiles at $Re_b \simeq 10500$. Near the porous wall it is seen that case Φ is most turbulent and the least turbulent one is case O though its wall-

normal permeability K_{yy} is approximately two order larger than the other cases. This indicates that although permeable surfaces relaxes the near-wall blocking effect on vortex motions and lead to strong turbulence, turbulence generation in the present cases is not very sensitive to the wall-normal permeability K_{yy}. Interestingly, rather than K_{yy}, small difference in K_{xx} seems to affect turbulence generation. (This trend does not change in the different Re_b cases.) Indeed, case Φ whose K_{xx} is 25% larger than that of case Θ is most turbulent and case O whose K_{xx} is 25% smaller than that of case Θ is least turbulent. When the ratio between the wall-normal and streamwise permeabilities is considered, the present cases are at K_{yy}/K_{xx} =1.2, 1.5 and 172.7. Thus, there might be a question about whether those trends are monotonic between the ratios of 1.5 and 172.7. Although the channel geometry was not the same as the present one, Matsuo *et al.* (2017) applied orthotropic porous media whose permeabilities were (K_{xx}, K_{yy}, K_{zz}) = (0.22, 0.17, 0.22) and (0.16, 0.97, 0.16) mm^2 to the bottom wall of turbulent rectangular duct flows and reported that turbulence was sensitive to the streamwise permeability rather than the the wall-normal permeability. Their permeability ratios were K_{yy}/K_{xx} =0.77 and 6.1. Hence, although the supporting data might not be enough, we consider that the presently observed trends are monotonic in the range of K_{yy}/K_{xx}=0.77-172.7.

For the flow underneath the porous surface, equation (3.7) suggests that the drag reduces as the streamwise permeability increases. Accordingly, the increase of K_{xx} leads to an increased flow rate enhancing the slippage velocity on the surface. This results in more relaxed shear rate $\partial[U]/\partial y$ near the surface. This is confirmed in figure 14 (a) that compares near-wall velocity profiles at $Re_b \simeq 10500$. Case O shows the largest velocity gradient followed by case Θ and then case Φ. Consequently, for the present cases, it is considered that relaxing the wall-blocking effect on turbulence enhances turbulence generation significantly making up for the reduction by relaxing the velocity gradient. Indeed, as shown in figure 14 (b), the profiles of shear production $P_{12} = -[\overline{v'^2}]\partial[U]/\partial y$ of case Φ shows the largest level followed by those of cases Θ and O. Accordingly, although it might be expected that relaxing the wall-blocking effect is related to the wall-normal permeability, turbulence generation is not controlled by the wall-normal permeability .

To see the near-wall turbulence in more detail, figure 15 shows the distribution of the joint probability density function $p(u', v')$ at $y^{p+} = 15$ for $Re_b \simeq 10500$. Although the shape difference is not very drastic, the angles between the major and the streamwise axes are β =11.9°, 12.2° and 16.4° for cases O, Θ and Φ, respectively. The order of the angle magnitude corresponds to the order of K_{xx}. Here, the major axis is determined as the least square approximated line of plots of (u', v'). When the motions in the second and forth quadrants (Q2 and Q4) simultaneously have large streamwise and wall-normal fluctuations, β increases and thus β is a measure to see the strength of the wall-normal fluctuations. Interestingly, even though the wall-normal permeability is approximately two-order larger than the other cases, case O has the smallest β suggesting that its near-wall turbulence receives more the wall-blocking effect. For further discussions, the decomposed Reynolds shear stress profiles are investigated using the quadrant analysis method:

$$\overline{(uv)}_m = \frac{1}{\sum N_m} \sum (u'v')_m, \tag{3.12}$$

where subscript $m(= 1 - 4)$ corresponds to the quadrant event. Figure 16(a-c) compares the decomposed Reynolds shear stress profiles of cases O, Θ and Φ at $Re_b \simeq 10500$. In all the plots, it is obvious that the events in the second quadrant (Q2): ejections are most dominant. The contribution of the fourth quadrant (Q4): sweeps, is also larger and it tends to be nearly the same as that of Q2 as the position moves toward the

wall surface. For turbulence near a solid wall, Wallace *et al.* (1972) reported that Q4 was most dominant very close to the wall while Q2 overtook it as the location moved away from the wall. The previous study on isotropic porous media (Suga *et al.* 2011) also showed such a trend and the intersection points of Q2 and Q4 were at y^{p+}=30–100 for $Re_b \simeq$10000. However, the present cases only show the distributions after the intersections (if they exist). As seen in figure 16 (*d*) that compares the Q4 distributions, obviously the Q4 profile of case Φ is most negative. The levels of cases O and Θ are similar to each other close to the wall while that of case Θ becomes more negative away from the wall. This suggests that sweep motions tend to extend more away from the wall with the increase of the streamwise permeability. Since parts of wall penetrating vortices having large streamwise momentum are observed as the sweeps, the streamwise permeability becomes the primary factor to maintain strong near-wall rotating motions when the wall-normal permeability is sufficiently large. Because the wall penetrating fluid pushes out the same amount of fluid from the surface forming parts of the ejections, the profiles of the ejections are closely related to those of the sweeps. Therefore, the sweeps and the ejections are considerably affected by the streamwise permeability. This is one of the reasons why turbulence is looked controlled by the streamwise permeability in this study. However, when the permeability ratio becomes smaller as $K_{yy}/K_{xx} \ll 1.0$, a different trend might be observed.

3.2. *Streamwise-spanwise plane measurements*

For understanding the turbulence fields more in details, streamwise-spanwise plane measurements are carried out and the spanwise structure is discussed. With the present experimental facility and measurement method, the two-dimensionality of the flow field and the reproducibility of the data between the x–y and x–z measurements are well confirmed as mentioned in section 2. The measured flows are at Re_b =3600, 4800, 10500, 13600 for case O, Re_b =3400, 5000, 10300, 13600 for case Θ and Re_b =3400, 5700, 10400, 13100 for case Φ.

3.2.1. *Snapshots of turbulence fields*

Figure 17(*a*) and (*b*) show examples of snapshots of the instantaneous streamwise velocity fluctuation u' indicating low- and high-speed fluid lumps observed at $y^{p+} \simeq 20$ for case O at $Re_b = 4800$ ($Re_K^* = 20.6$) and case Φ at $Re_b = 13100$ ($Re_K^* = 83.8$), respectively. The window size is $L_x/H \times L_z/H = 5.4 \times 2.6$ that corresponds to $L_x^{p+} \times L_z^{p+} = 2260 \times 1200$ and $L_x^{p+} \times L_z^{p+} = 6820 \times 3610$, respectively for figure 17(*a*) and (*b*). Clearly, large scale low- and high-speed fluid lumps are observed. The corresponding vorticity fields are shown in figure 17(*c,d*). In figure 17(*c*), there are fragments of shredded vortex tubes looking similar to those observed at a location under the structural transition range in the isotropic porous medium cases (Suga *et al.* 2017). This suggests that the condition of figure 17(*a,c*) is still under the transition range that is discussed later in section 3.2.2. Compared with figure 17(*a*), the fluid lumps look well aligned in the spanwise direction in figure 17(*b*). Their length×width is approximately $\Delta x^{p+} \times \Delta z^{p+} = 5000 \times 1300$. The observed patterns are very different from the longitudinally elongated streaks usually detected over solid smooth walls. Similar large scale fluid lumps were also observed in the isotropic porous medium cases over the transitional range and such patterns of fluid lumps were considered to be footprints of the spanwise transverse rolls which are considered to be generated by the K-H instability. Jiménez *et al.* (2001) suggested that a large scale perturbation is induced by the K-H instability associated with an inflection point of mean velocity profile at the surface of porous layer. In fact, the vorticity patterns seen in figure 17(*d*) look more regularly arranged and very similar to those indicated by the simulation

of Kuwata & Suga (2017). Since the pores of the present porous media are aligned with the coordinate axes as in the simulation, the footprints can be maintained more visibly than in the isotropic porous medium cases.

3.2.2. *Two-point correlations*

The normalized two-point correlation function:

$$\widehat{R_{ij}}(\Delta z) = \frac{R_{ij}(\Delta z)}{R_{ij}(0)} = \frac{\overline{u_i'(z)u_j'(z+\Delta z)}}{\overline{u_i'(z)u_j'(z)}}, \tag{3.13}$$

in the spanwise direction is applied to detect the spanwise scales of the structure. Figure 18 shows examples of $\widehat{R_{11}}(\Delta z)$ distributions. Figure 18(*a-c*) correspond to the results of case O at $Re_b = 4800$, case Θ at $Re_b = 10300$ and case Φ at $Re_b = 13100$, respectively. Although they are not very clear in figure 18(*a*), the distribution indicates short wavy profiles at locations closer to the wall surface as clearly shown in figure 18(*b,c*) for the higher Reynolds numbers. It has been confirmed that the wavelength of those short waves corresponds to the pore pitch of the EVA net shown in figure 1(*a*). However, as the wall-normal distance increases, those short waves disappear and local minimum in the profile becomes clearer. The depth of the local minimum and its positions change depending on the wall-normal distance.The locations of those local minima indicate the statistical spanwise distance between low-speed and neighbouring high-speed flow regions. Figure 19 shows the distributions of the spanwise spacing of streaks λ_z^{p+} against the wall-normal distance plus the zero plane displacement d with a curve that indicates the fitting line of the smooth solid-wall cases obtained from the literature (Smith & Metzler 1983; Iritani *et al.* 1985; Kim *et al.* 1987; Tomkins & Adrian 2003). Since the zero-plane displacement is a length scale associated with the penetration, $(y+d)^{p+}$ is an equivalent height to y^+ of smooth solid wall turbulence. It is seen that the points of λ_z^{p+} collapse around the curve under, $(y+d)^{p+}$=150–200 reasonably well. In the isotropic porous medium cases λ_z^{p+} also collapsed around the curve under $(y+d)^{p+} \simeq 100$ (Suga *et al.* 2017). They concluded that although the coherent streaky structure was disturbed, its characteristics were still maintained in such a region. This suggests that as seen in figure 17(*c*) whose location corresponds to $(y+d)^{p+} \simeq 105$, the structure observed in the present study may retain some of the characteristics of the coherent streaky structure at such a location which is a little higher than that of the isotropic porous medium case. At a position over a certain distance from the wall surfaces of $(y+d)^{p+}$ =150–200, the plotted values start to deviate largely from the correlation line. Above this structural transition region, the quasi-streaky structure is smeared out and no longer exist as it can be also confirmed in figure 17(*d*) whose location corresponds to $(y+d)^{p+} \simeq 380$. Since as discussed in section 3.1.2, the zero plane displacement d has a correlation with the generalized permeability Reynolds number Re_K^* (and the surrogate permeability Reynolds number Re_K^{**}), the observed structural change certainly correlates with the streamwise permeability.

For the discussion of the streamwise length of the fluid lumps, figure 20(*a, b*) shows examples of the distribution profiles of $\widehat{R_{11}}(\Delta x)$. Although it is possible to detect the local minima and maxima of the profiles in some cases as seen in figure 20(*b*), generally it is impossible to do so as seen in figure 20(*a*). This is because some small fluid lumps are irregularly detected between large fluid lumps and hence the averaging blurs their correlation $u_i'(x)u_j'(x+\Delta x)$. It can be considered that a part of those fluid lumps are produced by the instability with high wave number motions. By performing a linear stability analysis on free surface flows over porous media, Camporeale *et al.* (2013) classified the instability modes into three categories: namely, the surface, shear and porosity induced

modes. In the porosity induced instability mode, there are three sub-categories: stable, unstable and one caused by the interaction with the free surface. Although detecting the waves by those instability modes by spectrum analysis is desirable, it is impossible by the present sampling rate of 4 Hz. Accordingly, we focus on detecting the lowest streamwise wave number motions, which may correspond to the surface mode, by a two-point correlation function of spanwise averaged fluctuating velocities. Its definition is

$$\widehat{\langle R_{ij}\rangle}_z(\Delta x) = \frac{\overline{\langle u_i'(x)\rangle_z \langle u_j'(x+\Delta x)\rangle_z}}{\overline{\langle u_i'(x)\rangle_z \langle u_j'(x)\rangle_z}}, \tag{3.14}$$

where $\langle u_i'(x)\rangle_z$ is the spanwise averaged instantaneous fluctuating velocity. By this process, the contribution from the noisy smaller fluid lumps is reasonably damped. See the samples of the spanwise averaged fluctuating velocities in the lower images of figure 17(a,b).

The distribution profiles of $\widehat{\langle R_{11}\rangle}_z(\Delta x)$ shown in figure 20(c,d) correspond to the cases shown in figure 20(a, b). Clearly, it is now possible to detect local minima (and maxima) by this method though the magnitudes of local minima and maxima tend to reduce as the wall-normal distance increases due to the complexity of the structure. Since the location of the local minimum indicates the statistical streamwise distance between low-speed and neighbouring high-speed flow regions, it corresponds to the half of the wavelength λ_x of a transverse wavy motion. As discussed in the DNS studies of porous wall turbulence by Jiménez *et al.* (2001); Breugem *et al.* (2006); Kuwata & Suga (2016a, 2017), such a wavy motion is large-scale perturbation induced by the K-H instability as hypothesized by Raupach *et al.* (1991) and Finnigan (2000). It was also observed in the experiments of vegetation turbulence by Raupach *et al.* (1996); Finnigan (2000); Ghisalberti & Nepf (2002); Poggi *et al.* (2004). Figure 20(c) also indicates that it tends to be difficult to detect the location of the local minimum depending on the wall-normal distance since the structure cannot be stable all along the channel height. Hence, the K-H wavelength λ_x is estimated by the local minimum at a closer location of the wall-normal distance. Figure 21 shows the distribution of λ_x, which is detected from the $\widehat{\langle R_{11}\rangle}_z(\Delta x)$ profiles, against the shear Reynolds number $Re_\tau = u_\tau^p \delta_p/\nu$. Here, δ_p is the equivalent boundary layer thickness defined as $\delta_p/H = (u_\tau^p)^2/[(u_\tau^p)^2 + (u_\tau^t)^2]$, where u_τ^t is the friction velocity at the top smooth wall. Figure 21 also includes the DNS results of Breugem *et al.* (2006); Kuwata & Suga (2016a, 2017) and the presently processed results using the isotropic porous medium data of Suga *et al.* (2017) to see the general trend. The plotted points of Breugem *et al.* (2006); Kuwata & Suga (2016a) are for isotropic porous media while the data of Kuwata & Suga (2017) are for anisotropic porous media. It is confirmed that the DNS results distribute in the range of the presently measured data.

In the fully developed mixing layers, the normalized wavelength of the K-H-type coherent eddies by the vorticity thickness C_λ ($= \lambda_x/\delta_\omega$) is known to be $3.5 \leqslant C_\lambda \leqslant 5$ (Dimotakis & Brown 1976; Rogers & Moser 1994). For flows over the porous walls, the DNSs by Breugem *et al.* (2006); Kuwata & Suga (2016a, 2017) indicated $C_\lambda \simeq 3.4$ when the the boundary-layer thickness δ_p is considered to be equivalent to the vorticity thickness δ_ω while Raupach *et al.* (1996); Finnigan (2000) summarized that the best fitted value of C_λ was 4.05 for a wide range of turbulent canopy flows. As seen in figure 21, the experimental data collapse mainly around C_λ =5.5 and 4.3 and some data are around the line of C_λ =3.4, irrespective of anisotropy of the porous walls. This result of $3.4 \leqslant C_\lambda \leqslant 5.5$ for porous wall turbulence confirms that the characteristics of the K-H

waves over porous media are similar to those of the turbulent mixing layers though their detailed flow structures are very different.

4. Concluding summary

Three kinds of anisotropic porous media having large wall-normal permeabilities are made by piling up ethylene vinyl acetate copolymer nets with rounded-square shaped pores. Their wall permeability tensor is designed to have a larger wall-normal permeability than the other components and thus the ratios of the wall-normal to streamwise permeabilities are $K_{yy}/K_{xx} > 1.0$. Those porous media are constructed to have three mutually orthogonal principal axes and those principal axes are aligned with the Cartesian coordinate axes of the flow geometry. Correspondingly, their permeability tensors are diagonal. PIV measurements are performed for fully developed turbulent channel flows over those anisotropic porous media. Streamwise-wall-normal (x–y) and streamwise-spanwise (x–z) plane measurements are carried out at Re_b=900–13600. The obtained x–y plane data show that the streamwise permeability affects turbulence more significantly than the wall-normal permeability. To correlate the turbulence characteristics over isotropic and anisotropic porous wall flows a modified permeability Reynolds number, which is named the generalized permeability Reynolds number, is proposed considering the Kozeny-Carman equation. This generalized permeability Reynolds number is a function of the porosity and the streamwise permeability. For the general usage a surrogate permeability Reynolds number, which is essentially a modified pore Reynolds number and has a strong linear correlation with the generalized permeability Reynolds number, is also proposed. It is then confirmed that the generalized and surrogate permeability Reynolds numbers represent the turbulence characteristics over porous media, particularly for the zero plane displacement d and the roughness scale h of the log-law velocities, irrespective of anisotropy of porous media. From the discussion on the contributions of sweeps and ejections to the Reynolds shear stress near the porous media, it is confirmed that the streamwise permeability is the primary factor to affect sweeps and ejections which are the main events for the Reynolds shear stress. As the streamwise permeability increases, wall-penetrating vortices causing those events maintain more their strength. This results in the enhancement of turbulence over the present porous media.

From the x–z plane measurements, low- and high-speed streaks, which are similar to those of solid-wall turbulence, are also observed near the anisotropic porous walls. In case of a large Reynolds number, large-scale spanwise patterns which look similar to those observed in the numerical simulations by Kuwata & Suga (2017) are observed. They are confirmed to be from the transverse waves induced by the Kelvin-Helmholtz instability. It is also confirmed that near the anisotropic porous walls the spanwise spacing of the streaks well correlates with the wall normal distance plus the zero-plane displacement d of the log-law mean velocity profile. From the transitional range starting from $(y+d)^{p+} \simeq 200$ the quasi-coherent structure tends to be disturbed by the transverse rollers. This structural change is generally the same as that of the isotropic porous wall cases reported by Suga *et al.* (2017). Since the zero plane displacement d has a correlation with the generalized permeability Reynolds number, the observed structural change is certainly controlled by the streamwise permeability. Through the two-point correlation analysis of spanwise averaged instantaneous fields, it is found that the Kelvin-Helmholtz wavelength λ_x ranges in the region of λ_x/δ_p=3.4–5.5, where δ_p is the boundary layer thickness, irrespective of anisotropy of the porous walls. This range is generally accord with that of the turbulent mixing layers.

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Appendix A. Transport equations of turbulent and dispersion stresses in the double averaged system

In homogeneous porous media, the transport equation of the volume averaged Reynolds stress reads

$$
\begin{aligned}
&\frac{\partial \langle R_{ij}\rangle^f}{\partial t} + \langle \bar{u}_k\rangle^f \frac{\partial \langle R_{ij}\rangle^f}{\partial x_k} = \frac{\partial}{\partial x_k}\left(\nu \frac{\partial \langle R_{ij}\rangle^f}{\partial x_k}\right)\\
&-\frac{\partial}{\partial x_k}\left(\overline{\langle u_i'\rangle^f \langle u_j'\rangle^f \langle u_k'\rangle^f} + \overline{\langle \tilde{u}_i'\tilde{u}_j'\tilde{u}_k'\rangle^f}\right)\\
&-\frac{\partial}{\partial x_k}\left(\overline{\langle u_i'\rangle^f \langle \tilde{u}_j'\tilde{u}_k'\rangle^f} + \overline{\langle u_j'\rangle^f \langle \tilde{u}_i'\tilde{u}_k'\rangle^f} + \overline{\langle u_i'\rangle^f \langle \tilde{u}_j'\tilde{\bar{u}}_k\rangle^f} + \overline{\langle u_j'\rangle^f \langle \tilde{u}_i'\tilde{\bar{u}}_k\rangle^f}\right.\\
&\left.+\overline{\langle u_i'\rangle^f \langle \tilde{\bar{u}}_j\tilde{u}_k'\rangle^f} + \overline{\langle u_j'\rangle^f \langle \tilde{\bar{u}}_i\tilde{u}_k'\rangle^f} + \overline{\langle u_k'\rangle^f \langle \tilde{u}_i'\tilde{u}_j'\rangle^f} + \overline{\langle \tilde{\bar{u}}_k\tilde{u}_i'\tilde{u}_j'\rangle^f}\right)\\
&-\frac{1}{\rho}\left(\overline{\langle u_j'\rangle^f \frac{\partial \langle p'\rangle^f}{\partial x_i}} + \overline{\langle u_i'\rangle^f \frac{\partial \langle p'\rangle^f}{\partial x_j}} + \overline{\left\langle \tilde{u}_i' \frac{\partial \tilde{p}'}{\partial x_j}\right\rangle^f} + \overline{\left\langle \tilde{u}_j' \frac{\partial \tilde{p}'}{\partial x_i}\right\rangle^f}\right)\\
&-\langle R_{ik}\rangle^f \frac{\partial \langle \bar{u}_j\rangle^f}{\partial x_k} - \langle R_{jk}\rangle^f \frac{\partial \langle \bar{u}_i\rangle^f}{\partial x_k}\left(2\nu \overline{\frac{\partial \langle u_i'\rangle^f}{\partial x_k}\frac{\partial \langle u_j'\rangle^f}{\partial x_k}} + 2\nu\overline{\langle \frac{\partial \tilde{u}_i'}{\partial x_k}\frac{\partial \tilde{u}_j'}{\partial x_k}\rangle}\right)\\
&-\left\langle \left(\overline{\tilde{u}_i'\tilde{u}_k'} + \overline{\tilde{u}_i'\langle u_k'\rangle^f}\right)\frac{\partial \tilde{\bar{u}}_j}{\partial x_k}\right\rangle^f - \left\langle \left(\overline{\tilde{u}_j'\tilde{u}_k'} + \overline{\tilde{u}_j'\langle u_k'\rangle^f}\right)\frac{\partial \tilde{\bar{u}}_i}{\partial x_k}\right\rangle^f\\
&-\left\{\overline{-\langle \tilde{u}_k'\tilde{\bar{u}}_i\rangle^f \frac{\partial \langle u_j'\rangle^f}{\partial x_k}} - \overline{\langle \tilde{u}_k'\tilde{\bar{u}}_j\rangle^f \frac{\partial \langle u_i'\rangle^f}{\partial x_k}}\right\},
\end{aligned}
\tag{A 1}
$$

while the transport equation of the dispersion stress becomes

$$
\begin{aligned}
&\frac{\partial \langle T_{ij}\rangle^f}{\partial t} + \langle \bar{u}_k\rangle^f \frac{\partial \langle T_{ij}\rangle^f}{\partial x_k} = \frac{\partial}{\partial x_k}\left(\nu \frac{\partial \langle T_{ij}\rangle^f}{\partial x_k}\right)\\
&-\frac{\partial}{\partial x_k}\left(\left\langle \bar{\bar{u}}_j\overline{\langle u_k'\rangle^f \tilde{u}_j'}\right\rangle^f + \left\langle \bar{\bar{u}}_i\overline{\langle u_k'\rangle^f \tilde{u}_i'}\right\rangle^f\right)\\
&-\frac{\partial}{\partial x_k}\left(\langle 2\bar{\bar{u}}_i\bar{\bar{u}}_j\bar{\bar{u}}_k\rangle^f + \left\langle \bar{\bar{u}}_j\overline{\tilde{u_k}'\tilde{u}'}_i\right\rangle^f + \left\langle \bar{\bar{u}}_i\overline{\tilde{u_k}'\tilde{u}'}_j\right\rangle^f\right)\\
&-\frac{1}{\rho}\left(\frac{\partial \langle \bar{\bar{u}}_i\bar{\bar{p}}\rangle^f}{\partial x_j} + \frac{\partial \langle \bar{\bar{u}}_j\bar{\bar{p}}\rangle^f}{\partial x_i}\right) + \left\langle \frac{\bar{\bar{p}}}{\rho}\left(\frac{\partial \bar{\bar{u}}_i}{\partial x_j} + \frac{\partial \bar{\bar{u}}_j}{\partial x_i}\right)\right\rangle^f\\
&+\left\langle T_{ik}\frac{\partial \bar{\bar{u}}_j}{\partial x_k}\right\rangle^f + \left\langle T_{jk}\frac{\partial \bar{\bar{u}}_i}{\partial x_k}\right\rangle^f\\
&-\langle T_{ik}\rangle^f \frac{\partial \langle \bar{u}_j\rangle^f}{\partial x_k} - \langle T_{jk}\rangle^f \frac{\partial \langle \bar{u}_i\rangle^f}{\partial x_k} - 2\nu\left\langle \frac{\partial \bar{\bar{u}}_i}{\partial x_k}\frac{\partial \bar{\bar{u}}_j}{\partial x_k}\right\rangle^f
\end{aligned}
$$

$$-\left\{-\left\langle\left(\overline{\tilde{u}_i'\tilde{u}_k'}+\overline{\tilde{u}_i'\langle u_k'\rangle^f}\right)\frac{\partial\bar{\tilde{u}}_j}{\partial x_k}\right\rangle^f-\left\langle\left(\overline{\tilde{u}_j'\tilde{u}_k'}+\overline{\tilde{u}_j'\langle u_k'\rangle^f}\right)\frac{\partial\bar{\tilde{u}}_i}{\partial x_k}\right\rangle^f\right\}$$

$$-\overline{\langle\tilde{\bar{u}}_i\tilde{u}_k'\rangle^f\frac{\partial\langle u_j'\rangle^f}{\partial x_k}}-\overline{\langle\tilde{\bar{u}}_j\tilde{u}_k'\rangle^f\frac{\partial\langle u_i'\rangle^f}{\partial x_k}}+\bar{f}_i\langle\bar{u}_j\rangle^f+\bar{f}_j\langle\bar{u}_i\rangle^f. \quad (A\,2)$$

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Porous med.	φ	K_{xx} [mm^2]	K_{yy} [mm^2]	K_{zz} [mm^2]	C^F_{xx}[mm]	C^F_{yy}[mm]	C^F_{zz}[mm]
case O	0.7	0.044	7.6	0.044	0.025	1.91	0.025
case Θ	0.7	0.060	0.090	0.075	0.029	0.027	0.027
case Φ	0.7	0.075	0.090	0.060	0.027	0.027	0.029

TABLE 1. Characteristics of the anisotropic porous media; φ is the porosity; K_{xx}, K_{yy} and K_{zz} are the diagonal components of the permeability tensor; C^F_{xx}, C^F_{yy} and C^F_{zz} are the diagonal components of the coefficient of the Forchheimer tensor.

Porous med.	Re_b	Re_K	Re^*_K	Re^{**}_K	u^p_τ/u^t_τ	κ	d^{p+}	h^{p+}	$x-y$	$x-z$
case O	900	-	-	-	-	-	-	-	✓	
	1300	4.5	4.0	3.6	1.13	-	-	-	✓	
	3600	17.3	15.7	14.2	1.23	0.25	40	8.1	✓	✓
	4800	22.6	20.6	18.6	1.30	0.18	95	27.5	✓	✓
	10500	46.1	42.0	37.9	1.32	0.17	165	51.0	✓	✓
	13600	60.2	54.9	49.5	1.33	0.17	210	77.0	✓	✓
case Θ	3400	3.3	20.3	15.9	1.38	0.20	80	24.3	✓	✓
	5000	4.8	29.3	22.9	1.38	0.15	183	72.0	✓	✓
	10300	9.0	61.9	48.3	1.45	0.16	210	84.0	✓	✓
	13600	11.5	71.0	55.3	1.53	0.15	285	122.5	✓	✓
case Φ	3400	3.4	23.4	16.3	1.47	0.22	60	18.3	✓	✓
	5700	5.9	39.9	27.9	1.56	0.21	102	39.9	✓	✓
	10400	9.8	67.3	47.1	1.61	0.15	260	131.0	✓	✓
	13100	12.2	83.8	58.6	1.73	0.15	360	175.0	✓	✓

TABLE 2. Experimental conditions and measured parameters of the mean velocity fields; Re_b, Re_K, Re^*_K and Re^{**}_K are the bulk Reynolds number, the permeability Reynolds number defined by equation (3.3), the generalized permeability Reynolds number defined by equation (3.10) and the surrogate permeability Reynolds number defined by equation (3.11); u^t_τ and u^p_τ are the friction velocities on the top solid and bottom porous walls; κ, d and h are the von Kármán coefficient, the zero plane displacement and the roughness scale, respectively; $(\cdot)^{p+}$ corresponds to a value normalized by using u^p_τ.

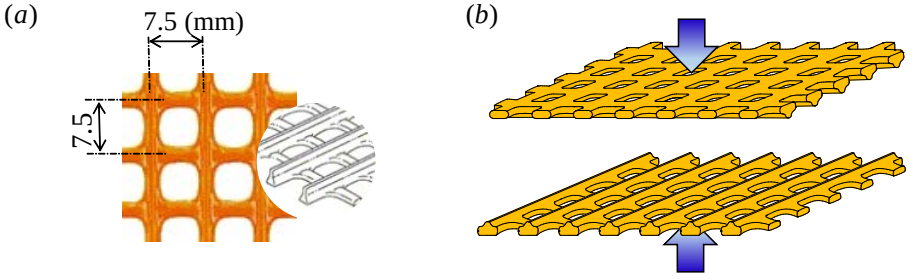

FIGURE 1. Polymer net for constructing the porous media; (*a*) shape of the EVA copolymer net (N-523, Takiron), (*b*) forming a unit layer.

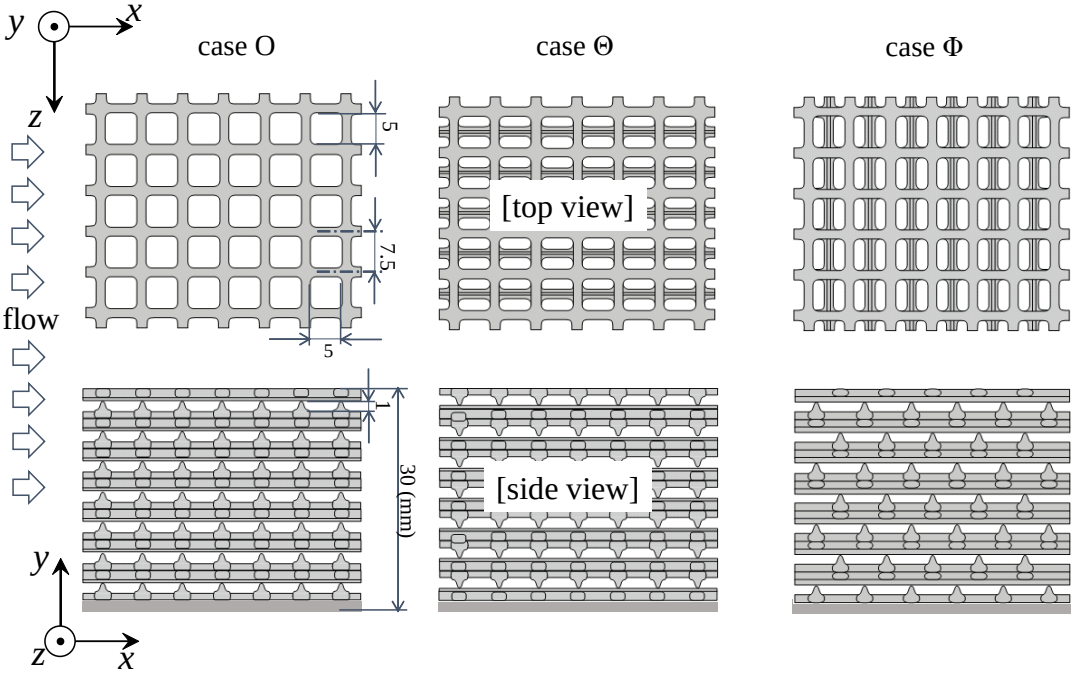

FIGURE 2. Three types of anisotropic porous media: cases O, Θ and Φ are named from the views of the meshes from the channel centre; lead plates are bonded to the very bottom layers to increase the weight.

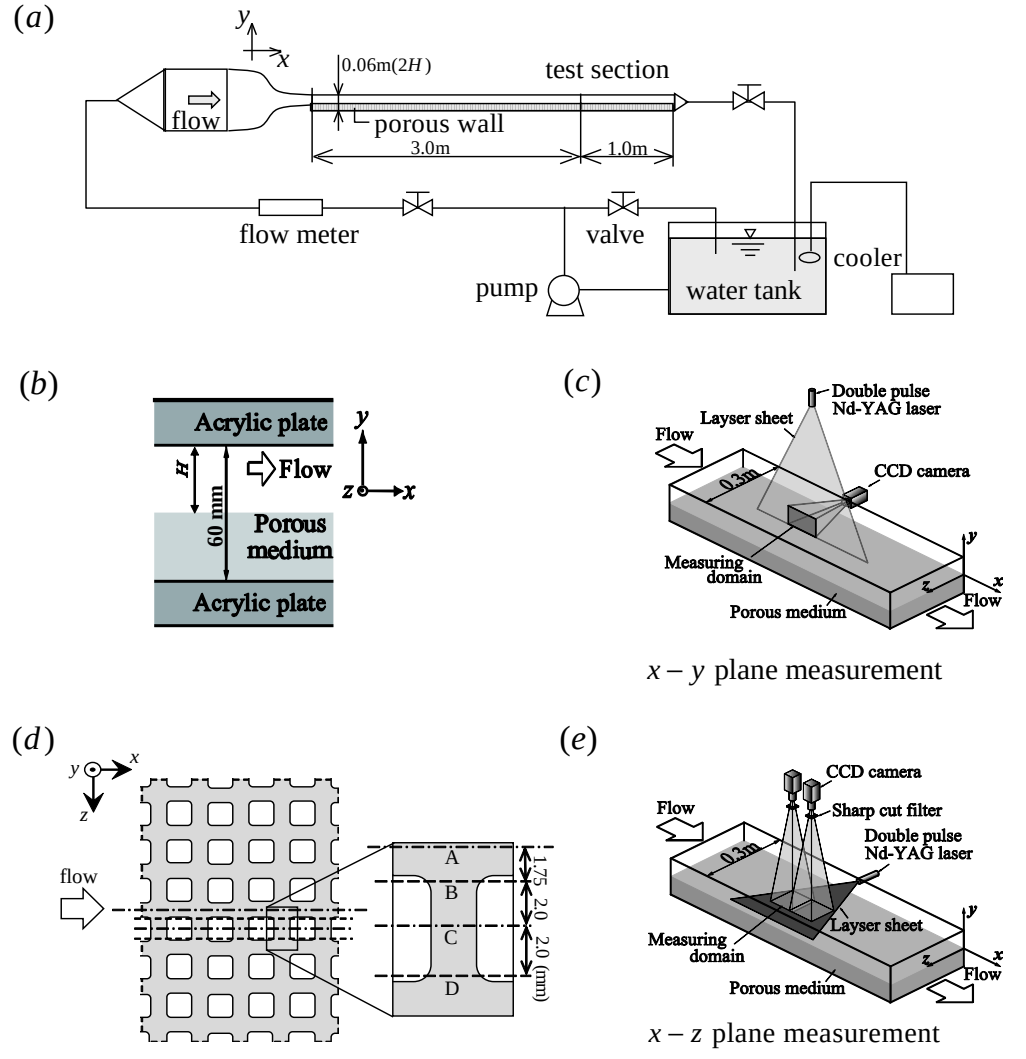

FIGURE 3. Experimental set up: (*a*) flow facility, (*b*) cross sectional view of the test section, (*c*) schematic view of the streamwise-wall-normal ($x-y$) plane measurements, (*d*) locations of the measured planes: A, B, C and D for volume averaging the $x-y$ plane measurements, (*e*) schematic view of the streamwise-spanwise ($x-z$) plane measurements.

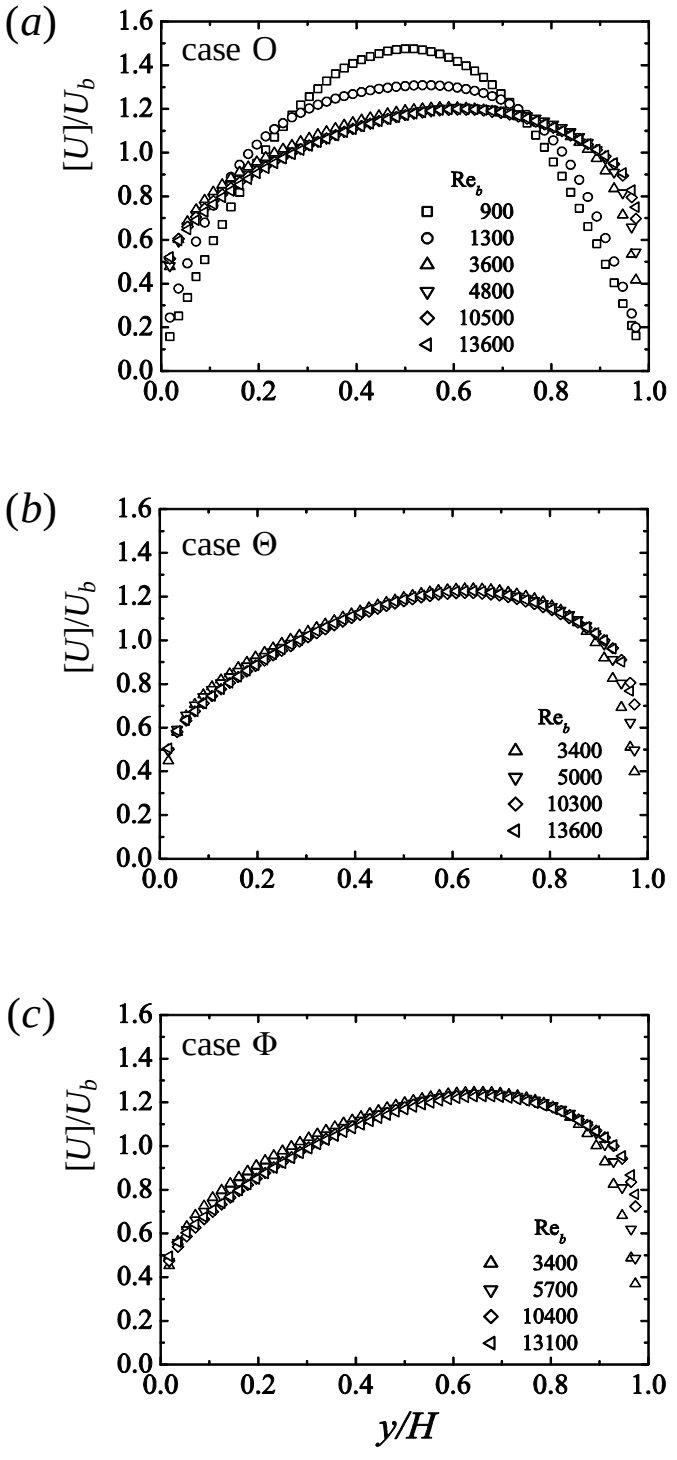

FIGURE 4. Mean velocity distributions: (*a*) case *O*, (*b*) case *Θ*, (*c*) case *Φ*.

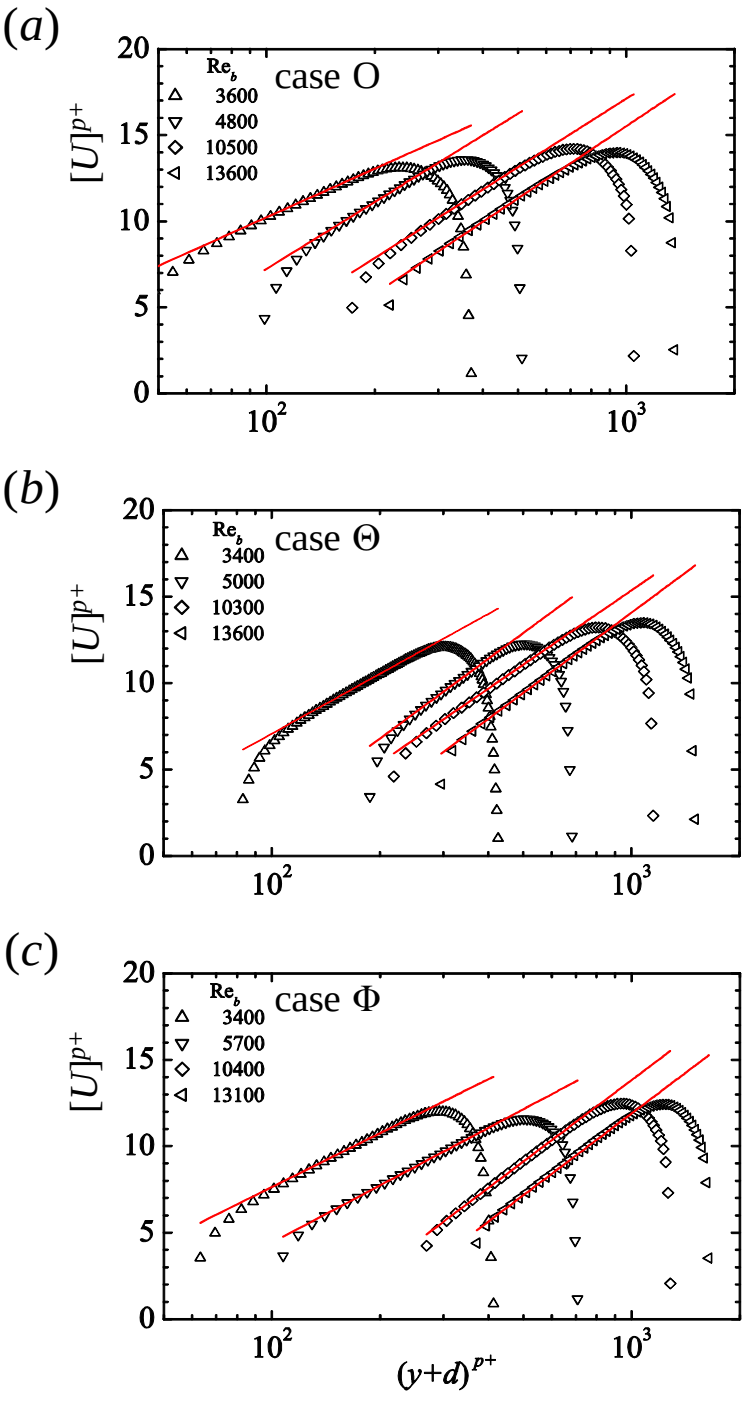

FIGURE 5. Mean velocity distributions in semi-log scale: (*a*) case *O*, (*b*) case *Θ*, (*c*) case *Φ*; lines are fitting lines.

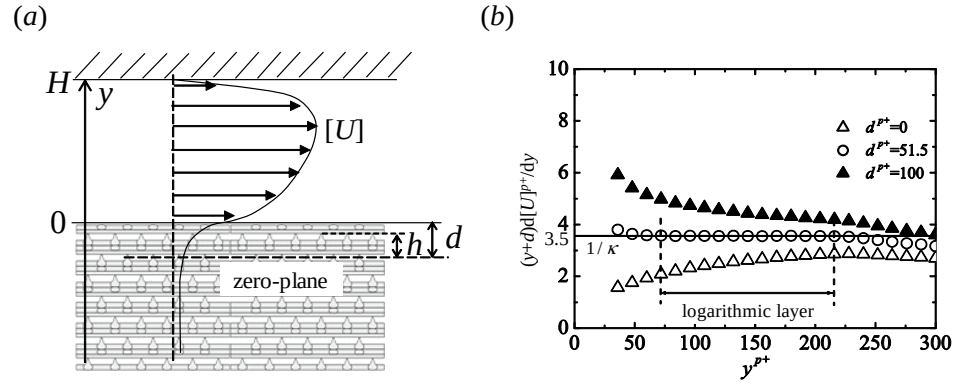

FIGURE 6. Parameters of mean velocity: (a) zero-plane displacement d and roughness length scale h, (b) logarithmic layer indicated by $(y+d)d\,[U]^{p+}/dy$.

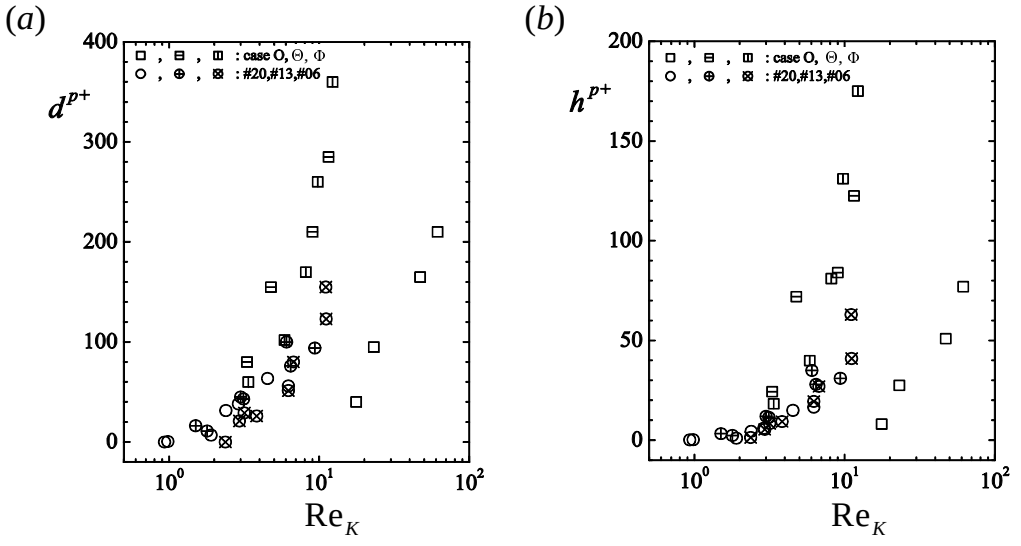

FIGURE 7. Distributions of log-law parameters against the permeability Reynolds number Re_K: (a) zero-plane displacement, and (b) roughness scale; #20, #13, #06 are the isotropic cases at $\varphi = 0.8$ of Suga *et al.* (2010, 2017).

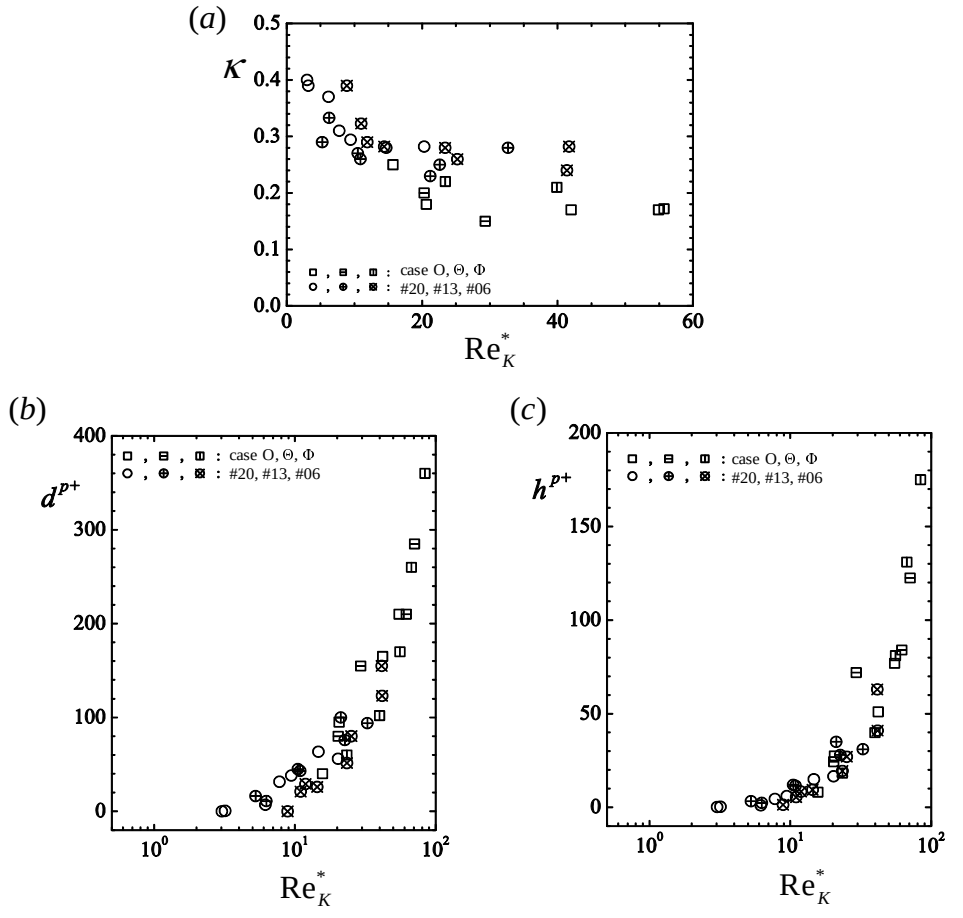

FIGURE 8. Distributions of log-law parameters against the generalized permeability Reynolds number Re_K^*: (*a*) von Kármán constant, (*b*) zero-plane displacement, and (*c*) roughness scale.

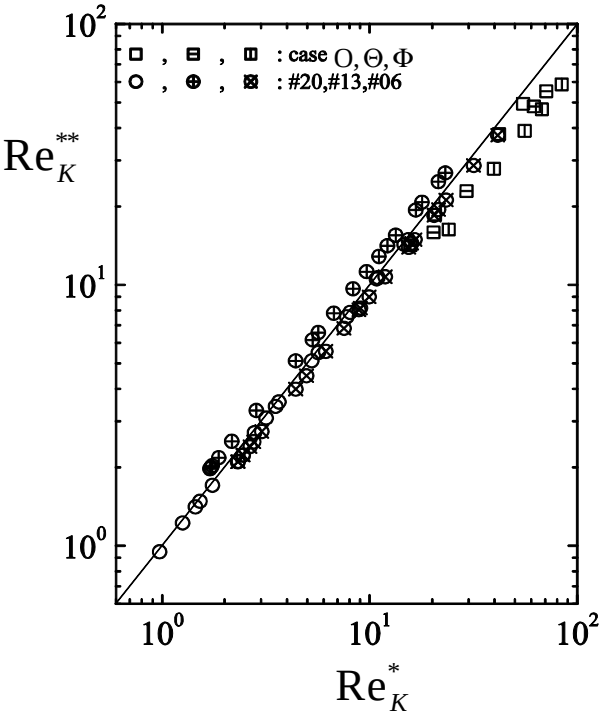

FIGURE 9. Correlation between the generalized and surrogate permeability Reynolds numbers.

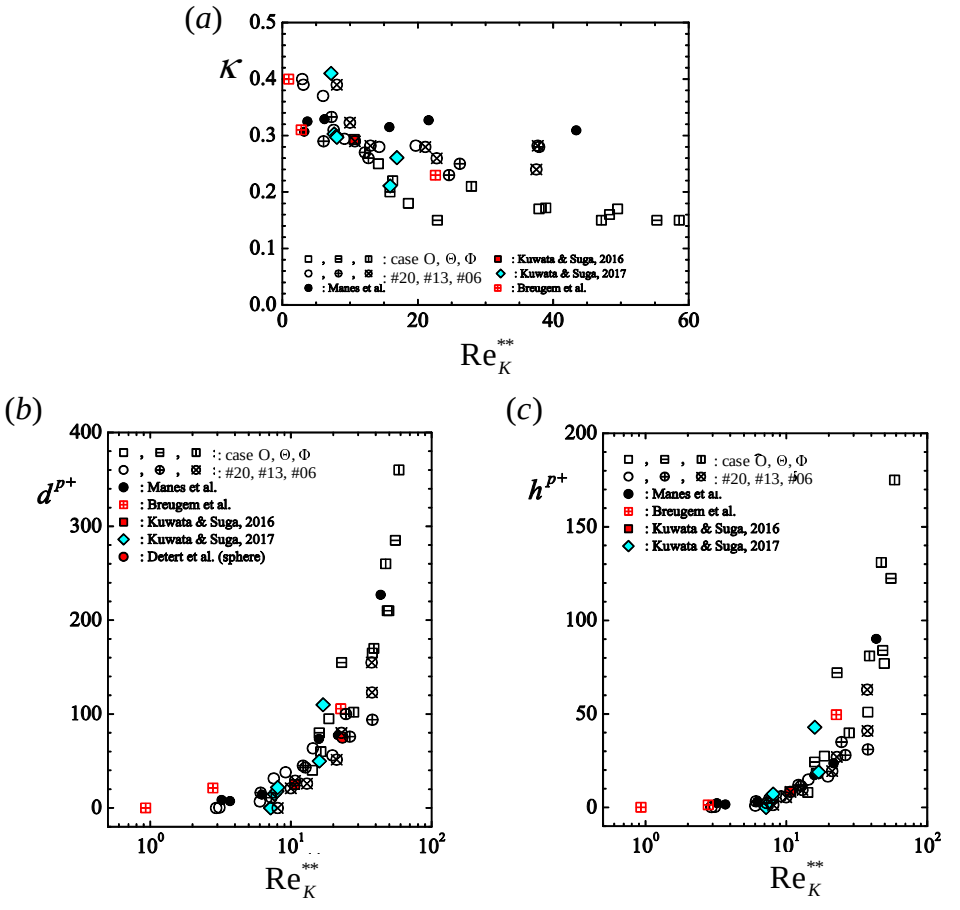

FIGURE 10. Distributions of log-law parameters against the surrogate permeability Reynolds number Re_K^{**}: (*a*) von Kármán constant, (*b*) zero-plane displacement, and (*c*) roughness scale; data of Detert *et al.* (2010); Manes *et al.* (2011); Breugem *et al.* (2006); Kuwata & Suga (2016*a*) are for isotropic porous media, data of Kuwata & Suga (2017) are for anisotropic porous media.

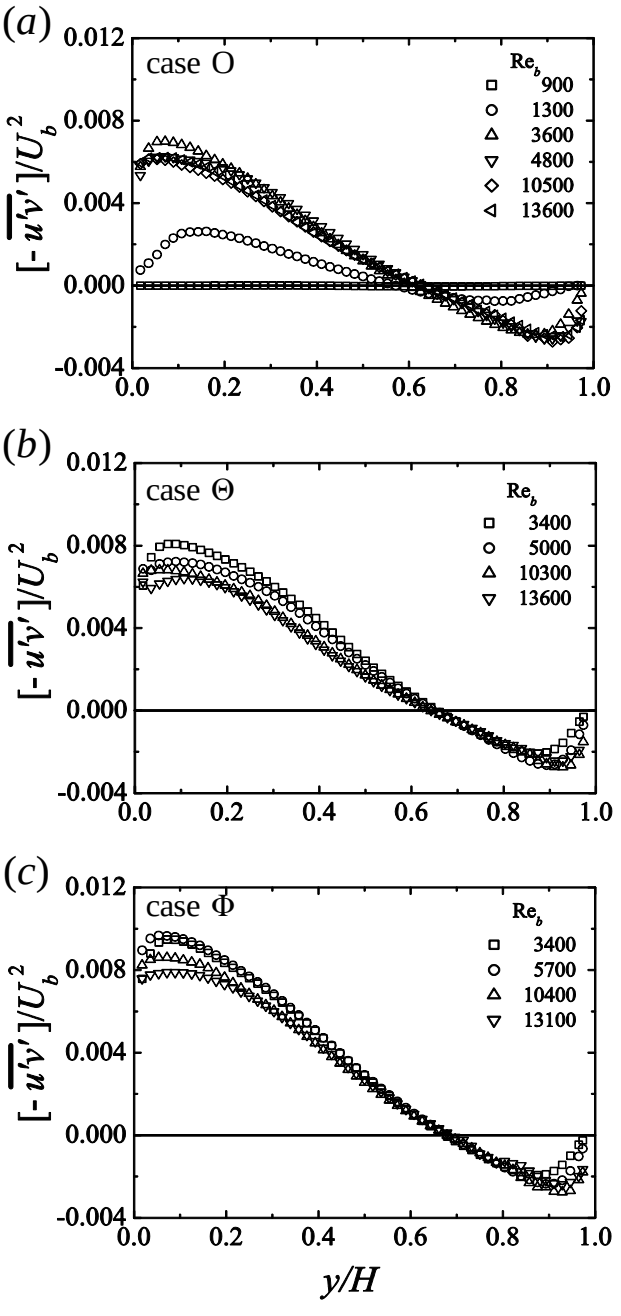

FIGURE 11. Comparison of Reynolds shear stress: (*a*) case *O*, (*b*) case *Θ*, (*c*) case *Φ*.

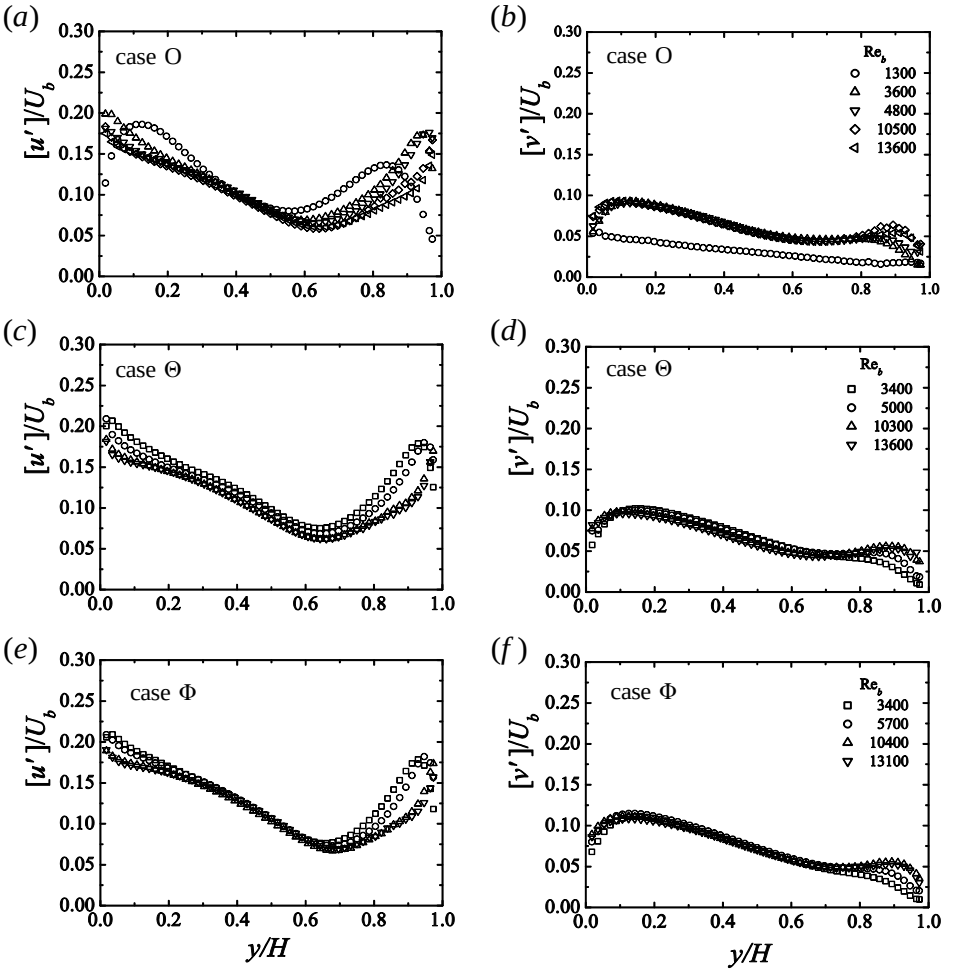

FIGURE 12. Comparison of turbulent intensities: (*a*) streamwise turbulent intensity of case O, (*b*) wall-normal turbulent intensity of case O, (*c*) streamwise turbulent intensity of case Θ, (*d*) wall-normal turbulent intensity of case Θ, (*e*) streamwise turbulent intensity of case Φ, (*f*) wall-normal turbulent intensity of case Φ.

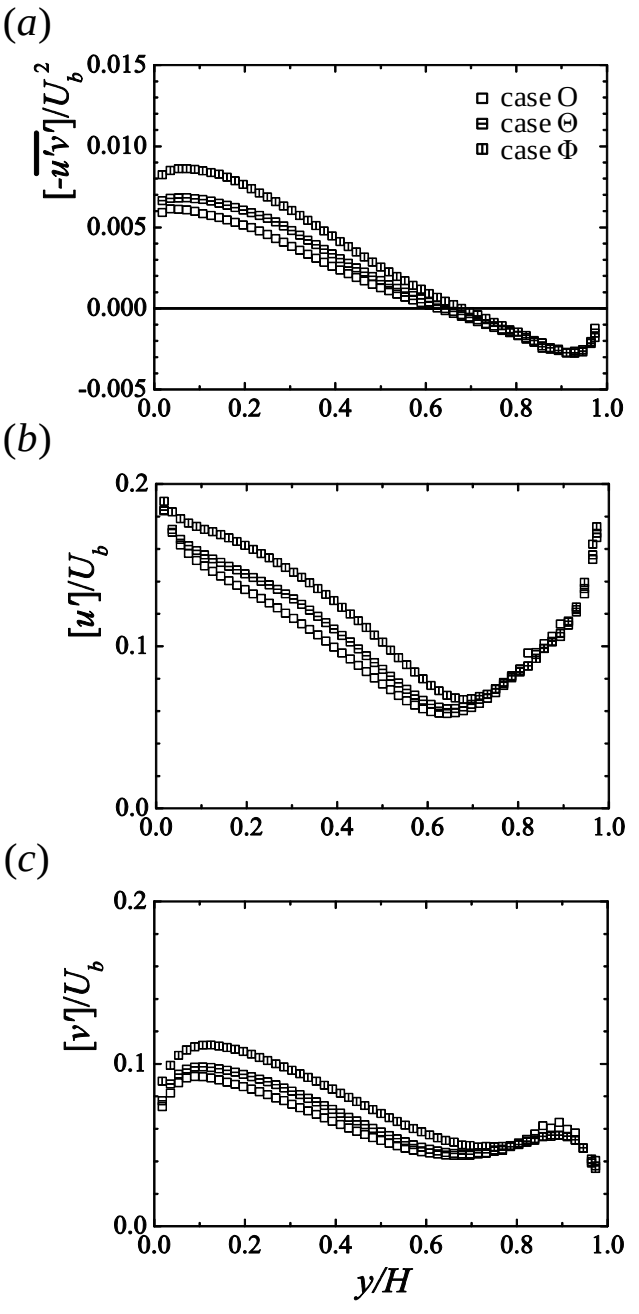

FIGURE 13. Comparison of turbulence quantities at $Re_b \simeq 10500$: (*a*) Reynolds shear stress, (*b*) streamwise turbulent intensity, (*c*) wall-normal turbulent intensity.

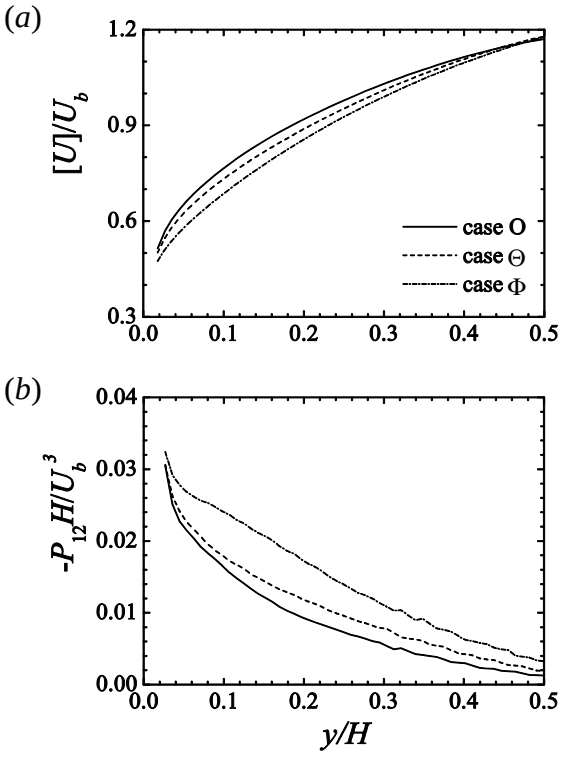

FIGURE 14. Comparison of mean velocity and shear production near the porous wall at $Re_b \simeq 10500$: (a) mean velocity profiles, (b) shear production $P_{12} = -[\overline{v'^2}]\partial[U]/\partial y$ profiles.

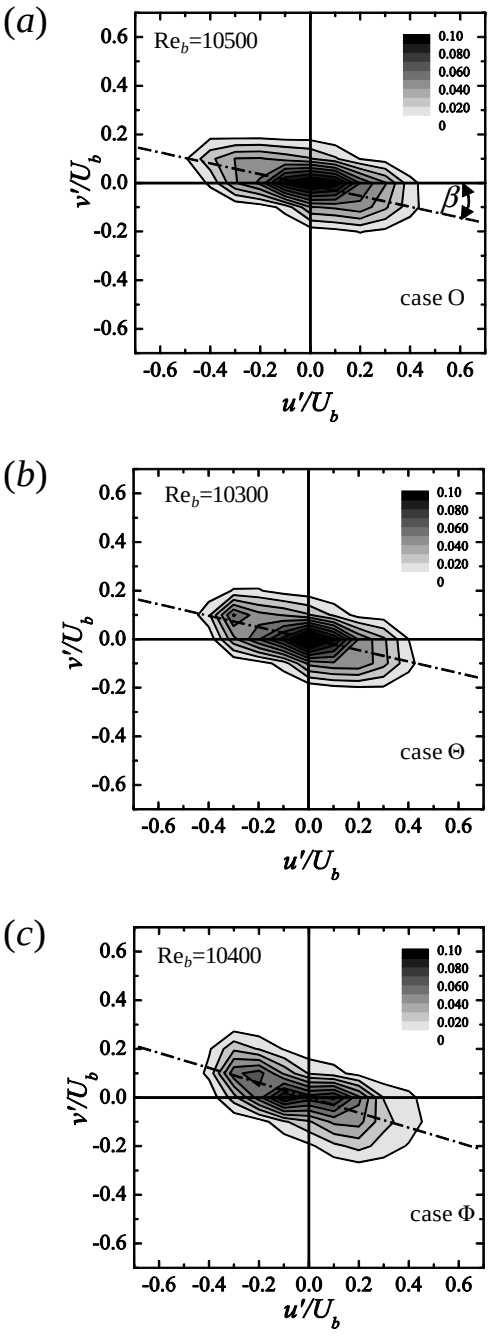

FIGURE 15. Joint probability density function $p(u', v')$ of fluctuating velocity at $y^{p+} = 15$ for $Re_b \simeq 10500$: (*a*) case O ($\beta = 11.9°$), (*b*) case Θ ($\beta = 12.2°$), (*c*) case Φ ($\beta = 16.4°$); β is the streamwise angle of the major axis of (u', v') distribution.

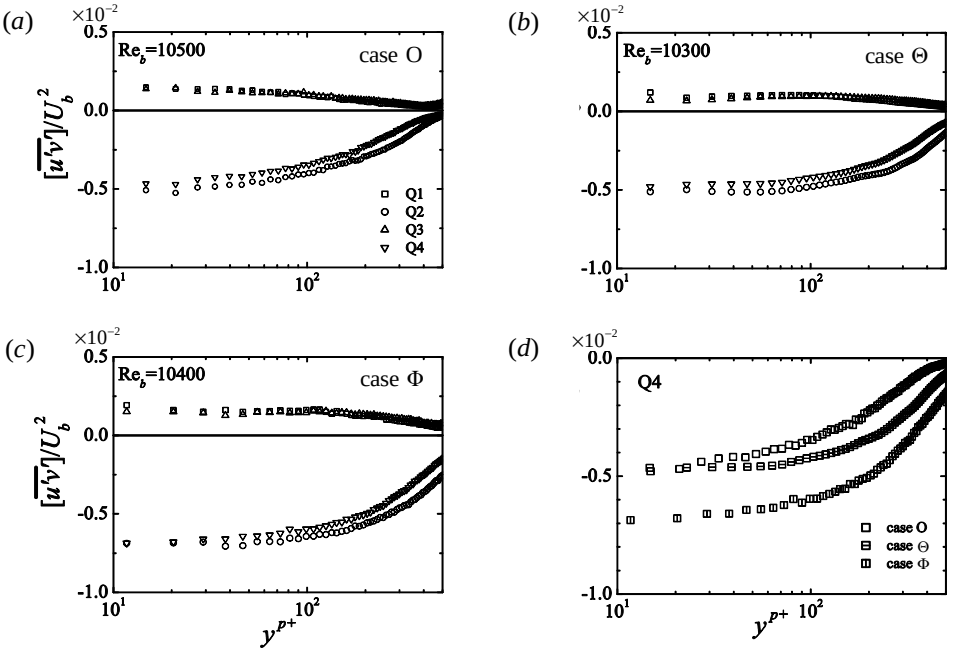

FIGURE 16. Quadrant analysis of the Reynolds shear stress distributions at $Re_b \simeq 10500$: (a) case O at $Re_b = 10500$, (b) case Θ at $Re_b = 10300$, (c) case Φ at $Re_b = 10400$, (d) comparison of sweeps: Q4.

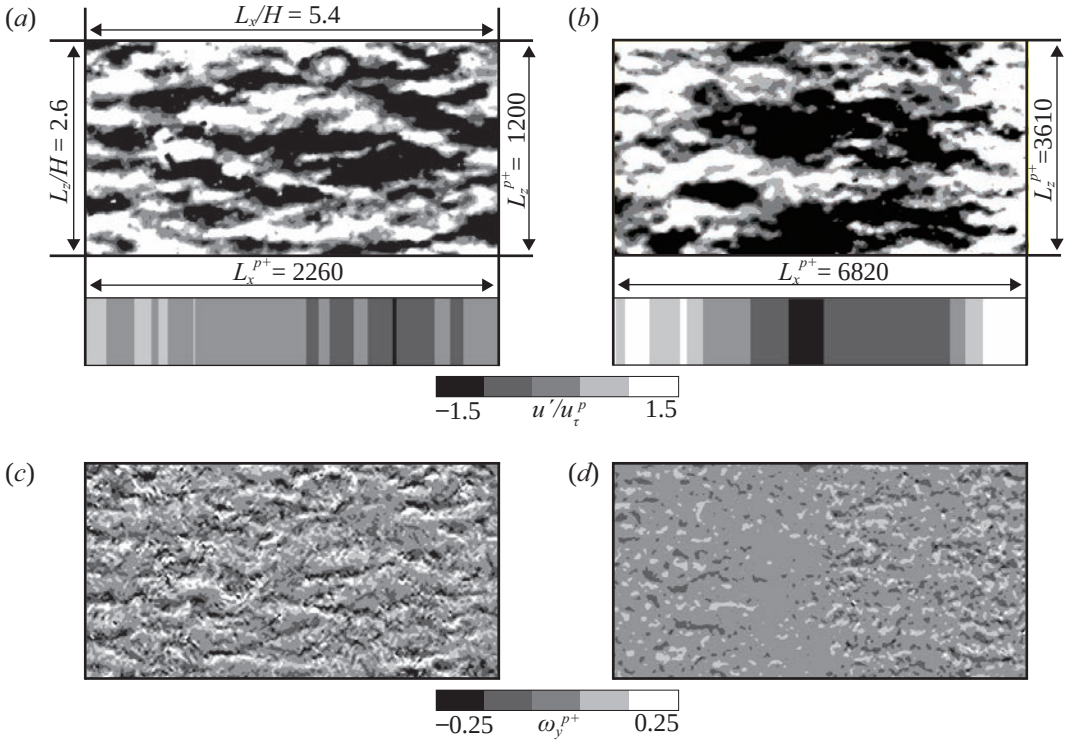

FIGURE 17. Snapshots of low- and high-speed fluid lumps at $y^{p+} \simeq 20$: (*a, b*) fluctuation velocity contours of case O at $Re_b = 4800, Re_K^* = 20.6$ and case Φ at $Re_b = 13100, Re_K^* = 83.8$, respectively. The upper images are snapshots of the instantaneous fields and the lower images correspond to the spanwise averaged fields of the upper images. (*c, d*) instantaneous wall-normal vorticity $\omega_y^{p+} = (\partial u/\partial z - \partial w/\partial x)\nu/(u_\tau^p)^2$ fields corresponding to the snapshots shown in (*a*) and (*b*), respectively.

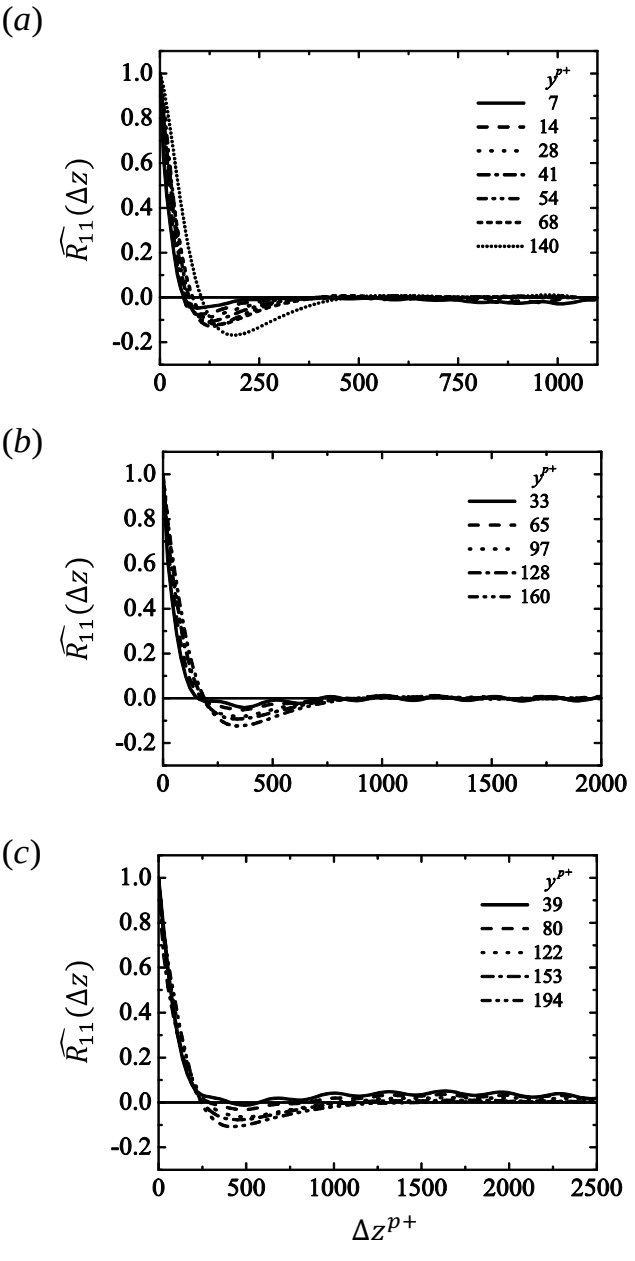

FIGURE 18. Two-point correlation of the streamwise velocity versus spanwise spacing: (*a*) case O at $Re_b = 4800$ ($Re_K^* = 20.6$), (*b*) case Θ at $Re_b = 10300$ ($Re_K^* = 61.9$), (*c*) case Φ at $Re_b = 13100$ ($Re_K^* = 83.8$).

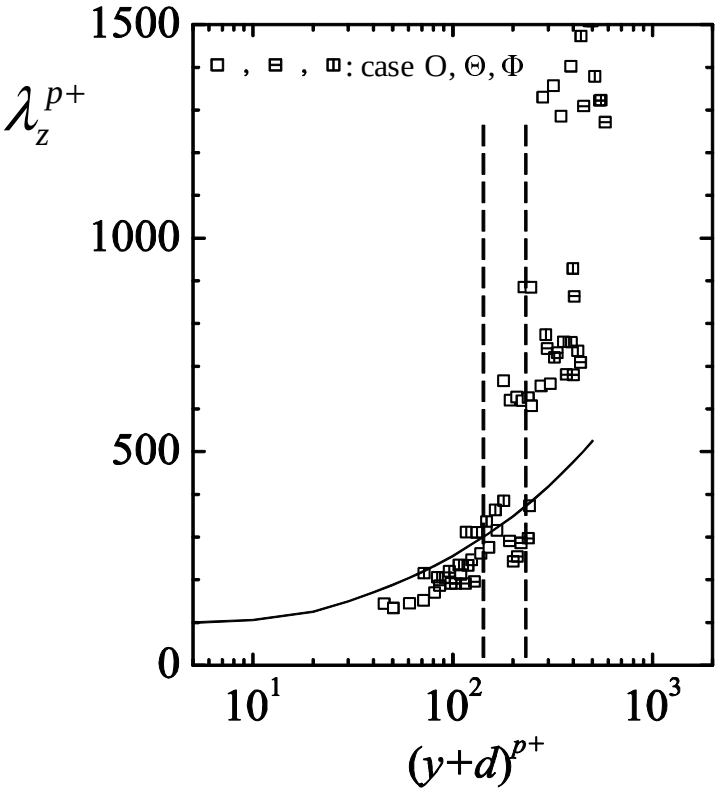

FIGURE 19. Distribution of spanwise spacing of streaks in the wall-normal direction; solid line indicates the fitting line of the solid-wall cases from the literature (Smith & Metzler 1983; Iritani *et al.* 1985; Kim *et al.* 1987; Tomkins & Adrian 2003) and broken lines indicate the transitional range.

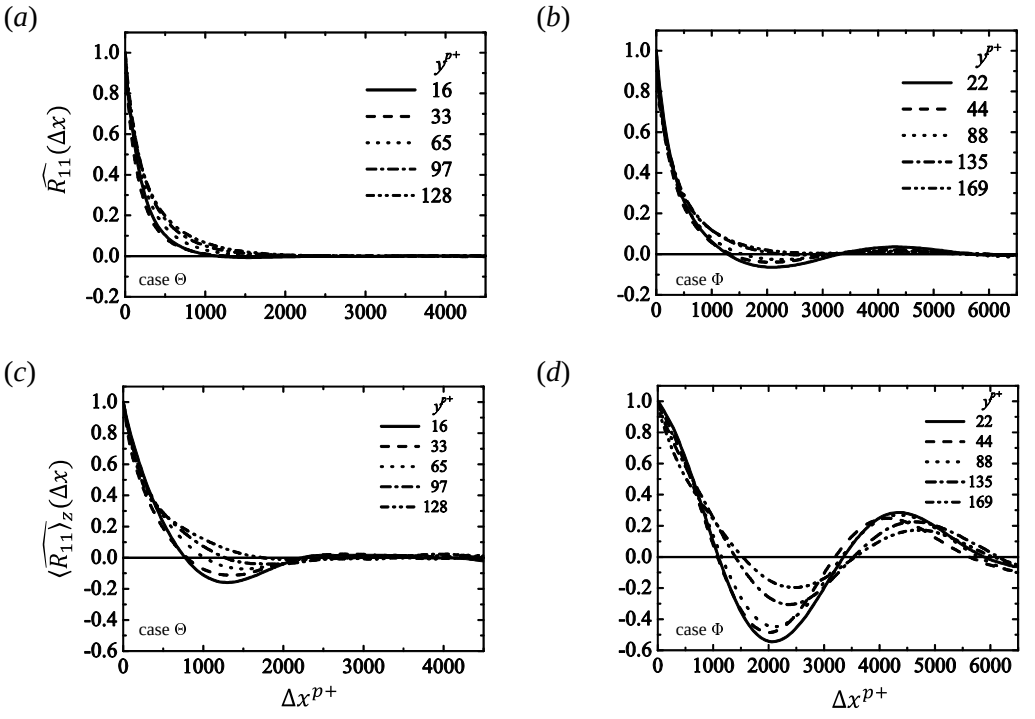

FIGURE 20. Two-point correlation of the streamwise velocity versus streamwise spacing: (*a*) standard two-point correlation functions $\widehat{R_{11}}(\Delta x)$ for case Θ at $Re_b = 10300$ ($Re_K^* = 61.9$), (*b*) two-point correlation functions of the spanwise averaged field $\widehat{\langle R_{11}\rangle}_z(\Delta x)$ for case Θ at $Re_b = 10300$, (*c*) standard two-point correlation functions $\widehat{R_{11}}(\Delta x)$ for case Φ at $Re_b = 13100$ ($Re_K^* = 83.8$), (*d*) two-point correlation functions of the spanwise averaged field $\widehat{\langle R_{11}\rangle}_z(\Delta x)$ for case Φ at $Re_b = 13100$.

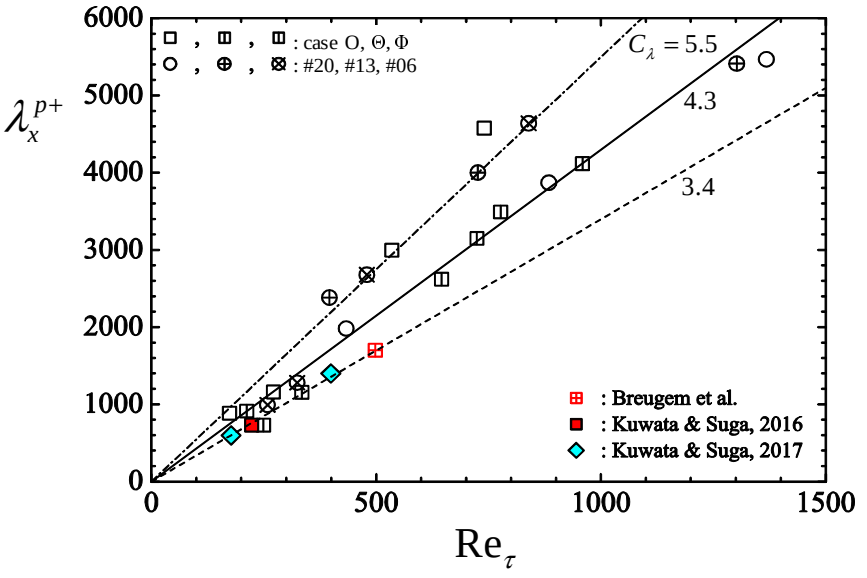

FIGURE 21. Streamwise wavelength of the fluid lumps; #20, #13, #06 are the isotropic cases of Suga *et al.* (2017), data of Breugem *et al.* (2006); Kuwata & Suga (2016*a*) are for isotropic porous media, data of Kuwata & Suga (2017) are for anisotropic porous media; chain, solid and broken lines correspond to $\lambda_x = C_\lambda \delta_p$ with C_λ =5.5,4.3 and 3.4, respectively.